

Formal methods for real-world systems: study of two cases

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Introduction

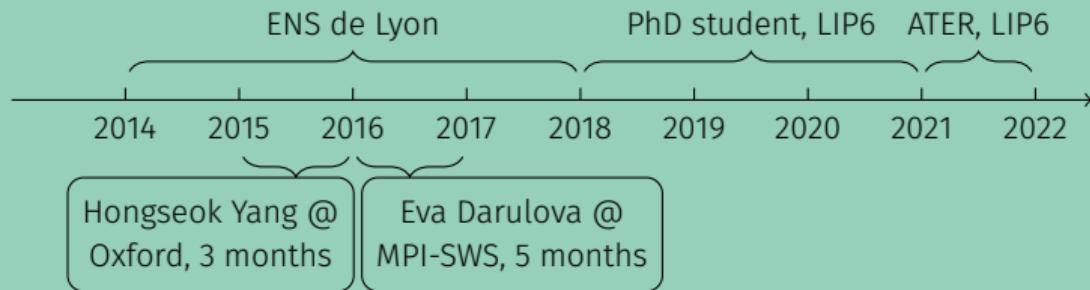
Introduction

Curriculum



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Curriculum



Research field: formal methods

⇒ Improve confidence in software.

Introduction

Curriculum



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⇒ Improve confidence in software.

Means

- ▶ Theory: formal definition and reasoning over systems
- ▶ Practice: software development

Introduction

Personal methodology

Constant back and forth between theory and practice

- 1 Find interesting bugs, properties or systems to study (GitHub, ...)
- 2 Theoretical study and solution
- 3 Implementation and experimental validation (on 1)

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- ▶ Python programs using C libraries ↽ static analysis
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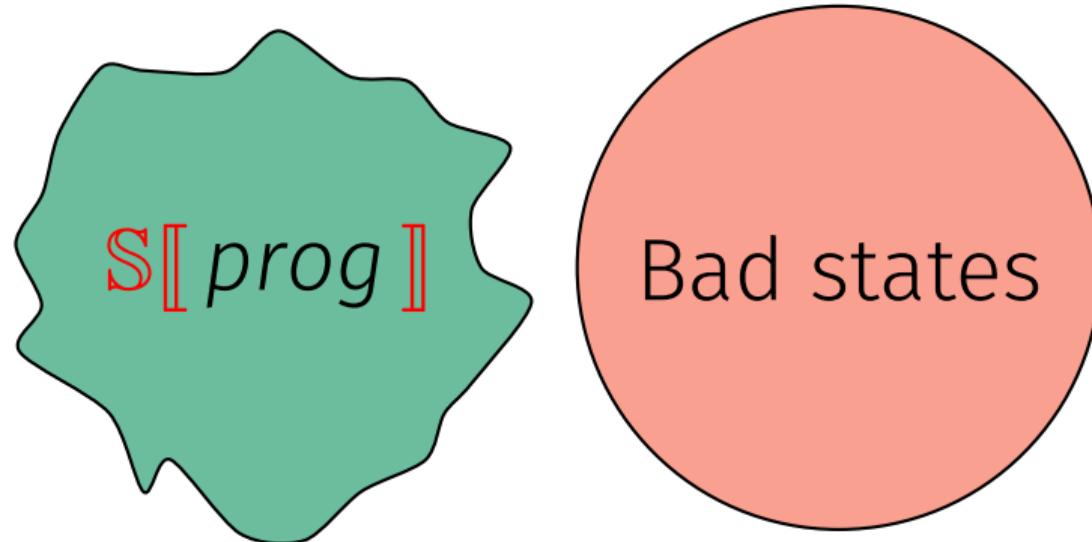
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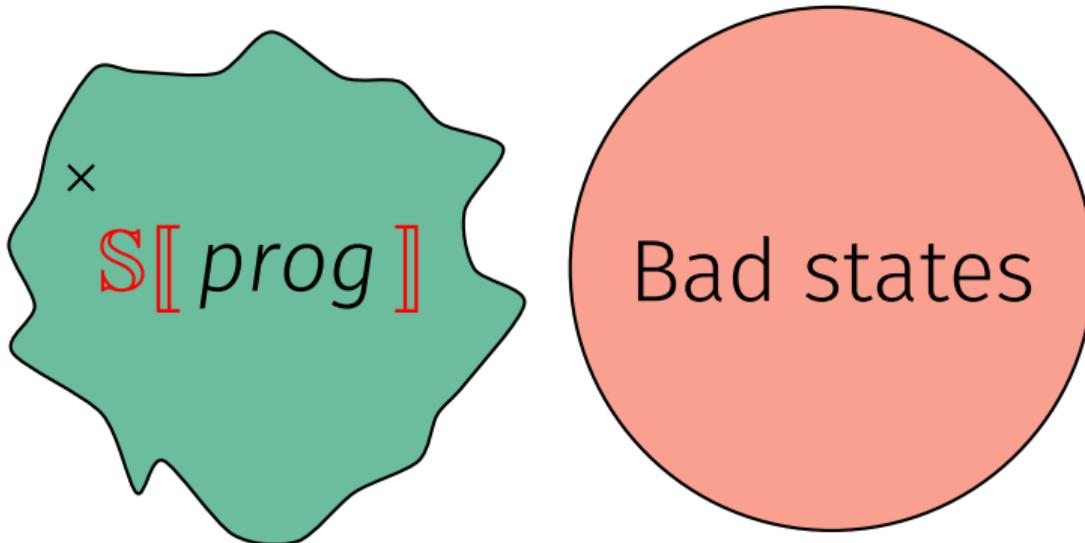
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- ▶ Python programs using C libraries ↵ static analysis
 - Abdelraouf Ouadjaout (LIP6)
 - Antoine Miné (LIP6)
- ▶ Implementation of the French tax code ↵ compiler, modernization
 - Denis Merigoux (Inria Prosecco)
 - Jonathan Protzenko (MSR)

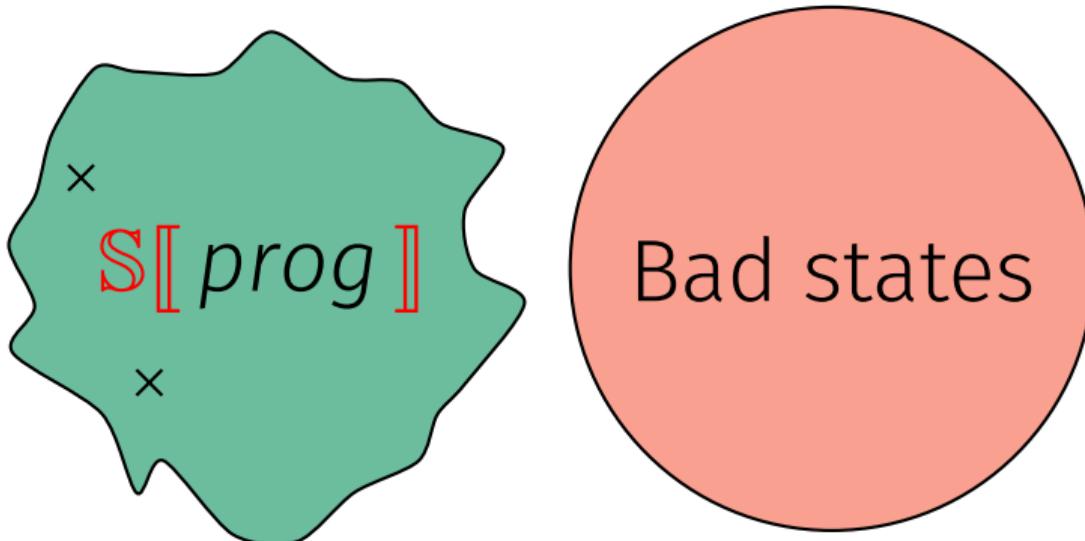
Software verification



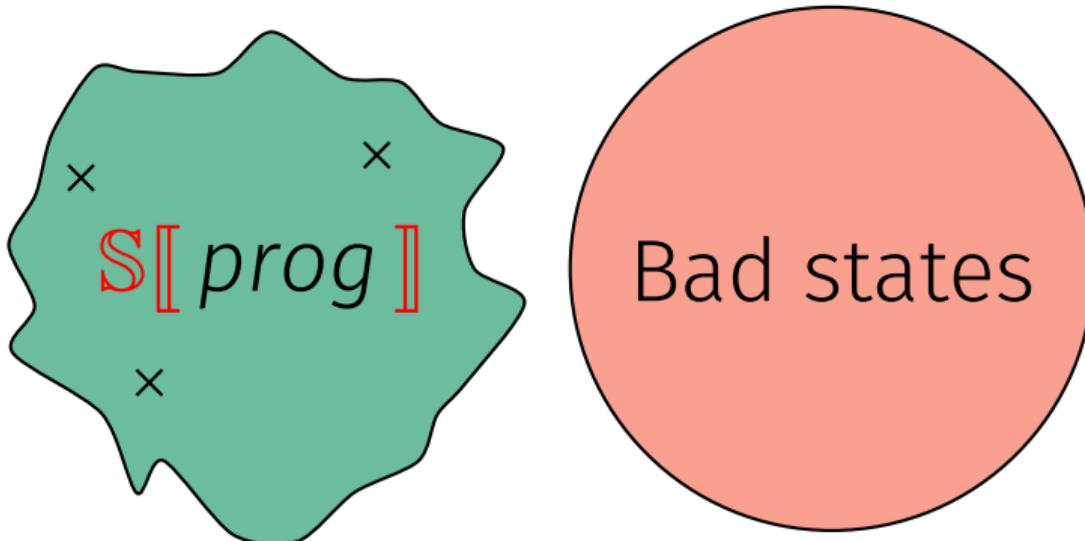




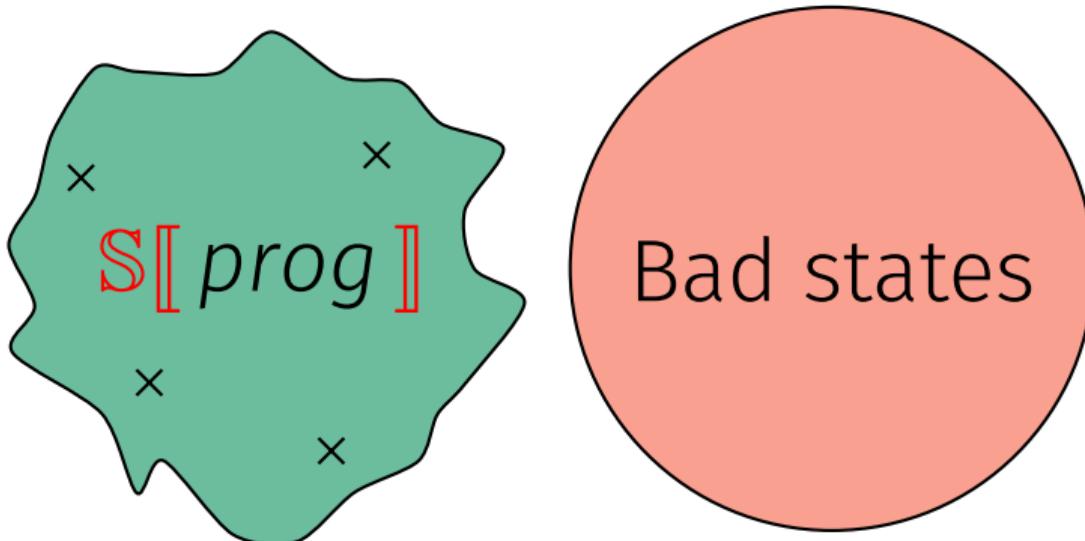
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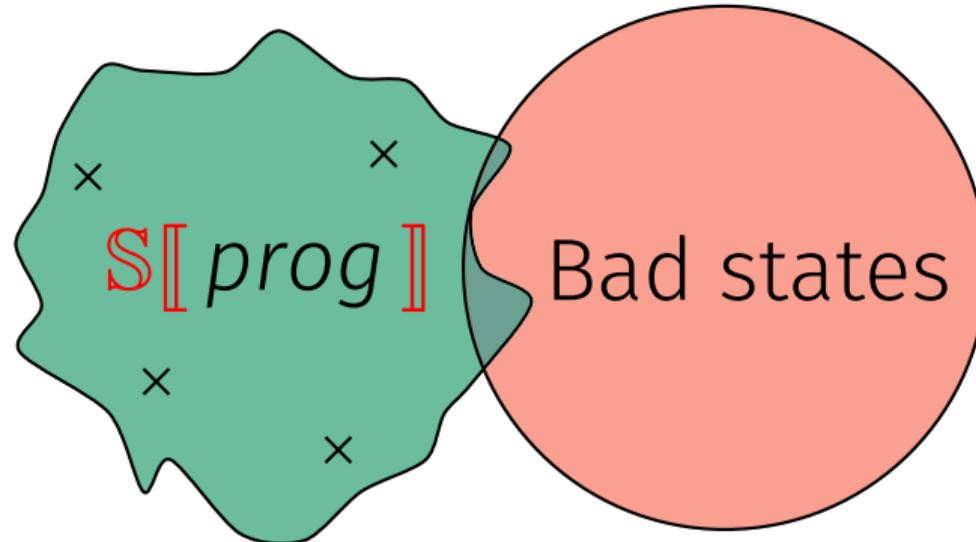
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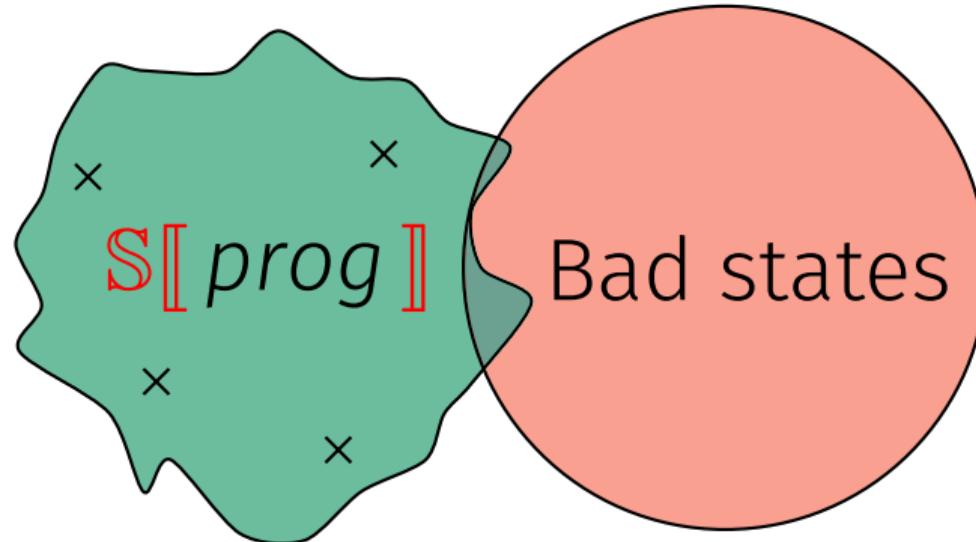
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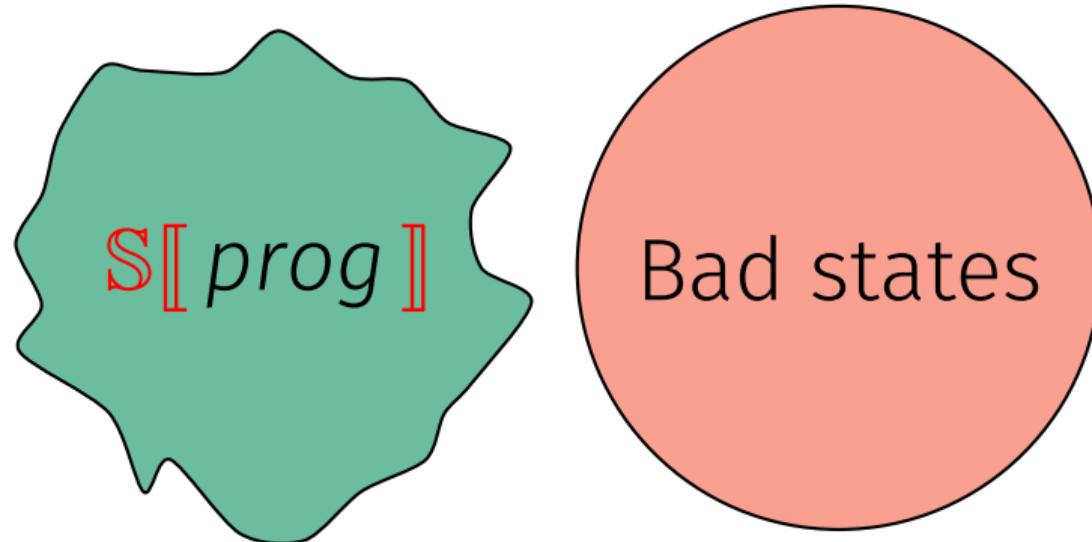
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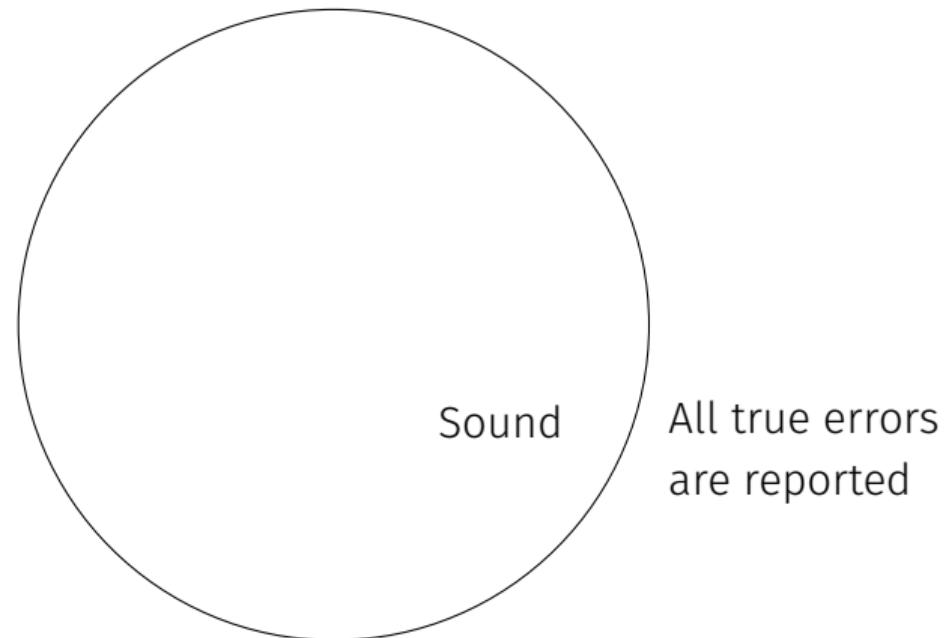
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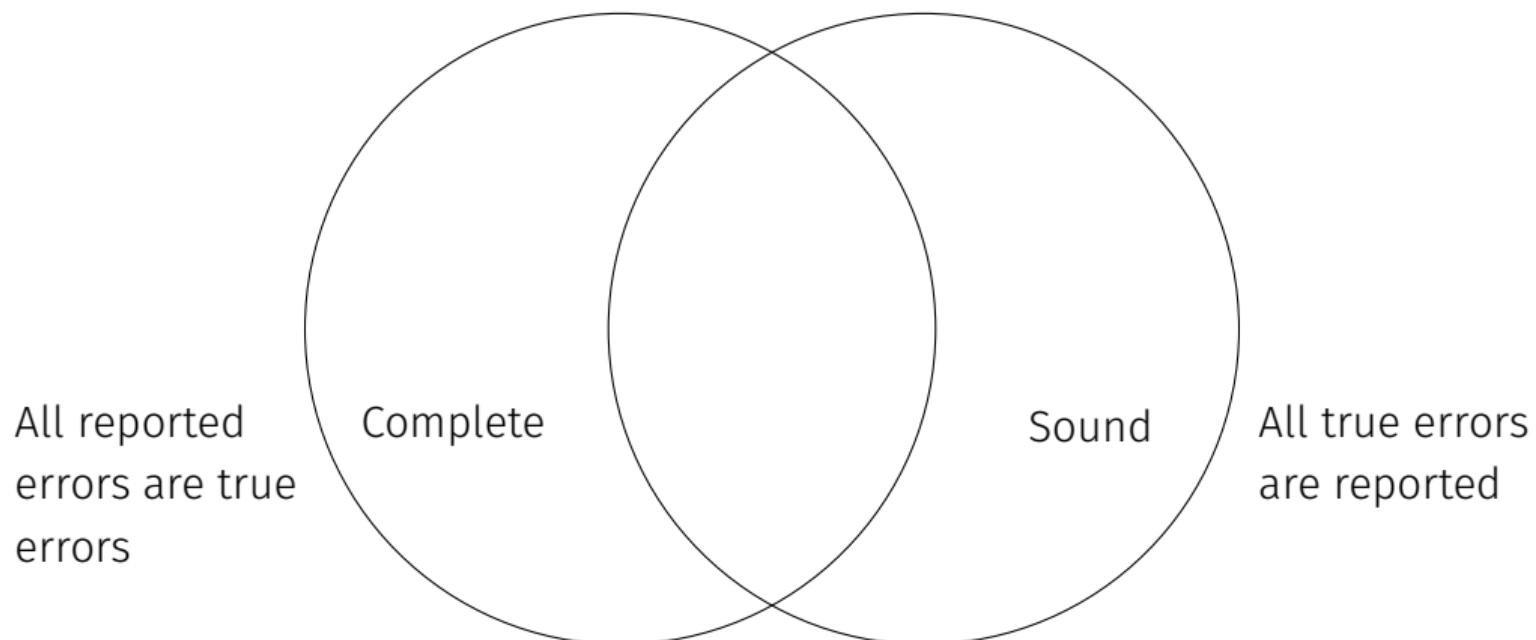
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Would there be a way to automatically prove programs correct?

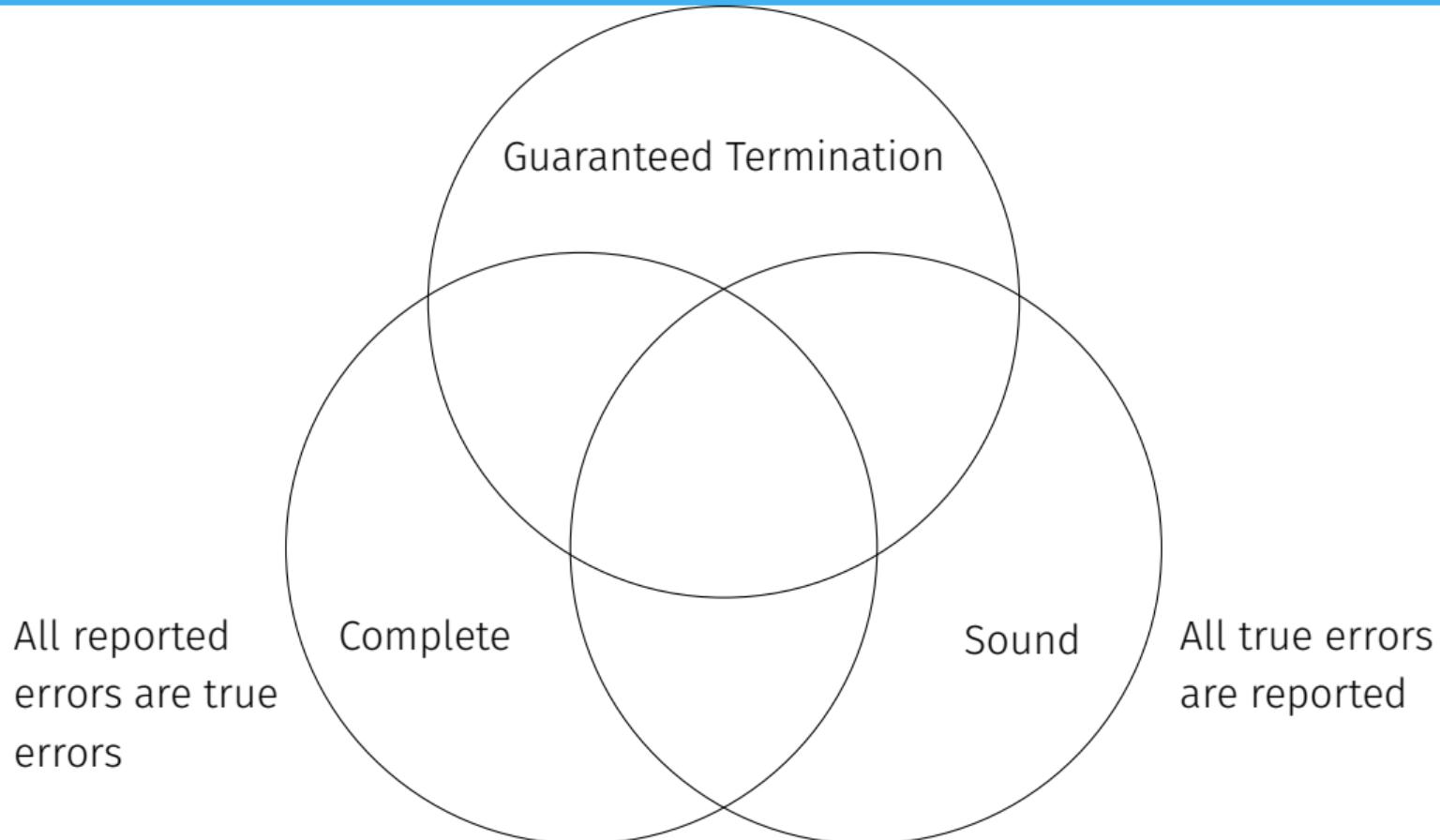
An impossibility theorem



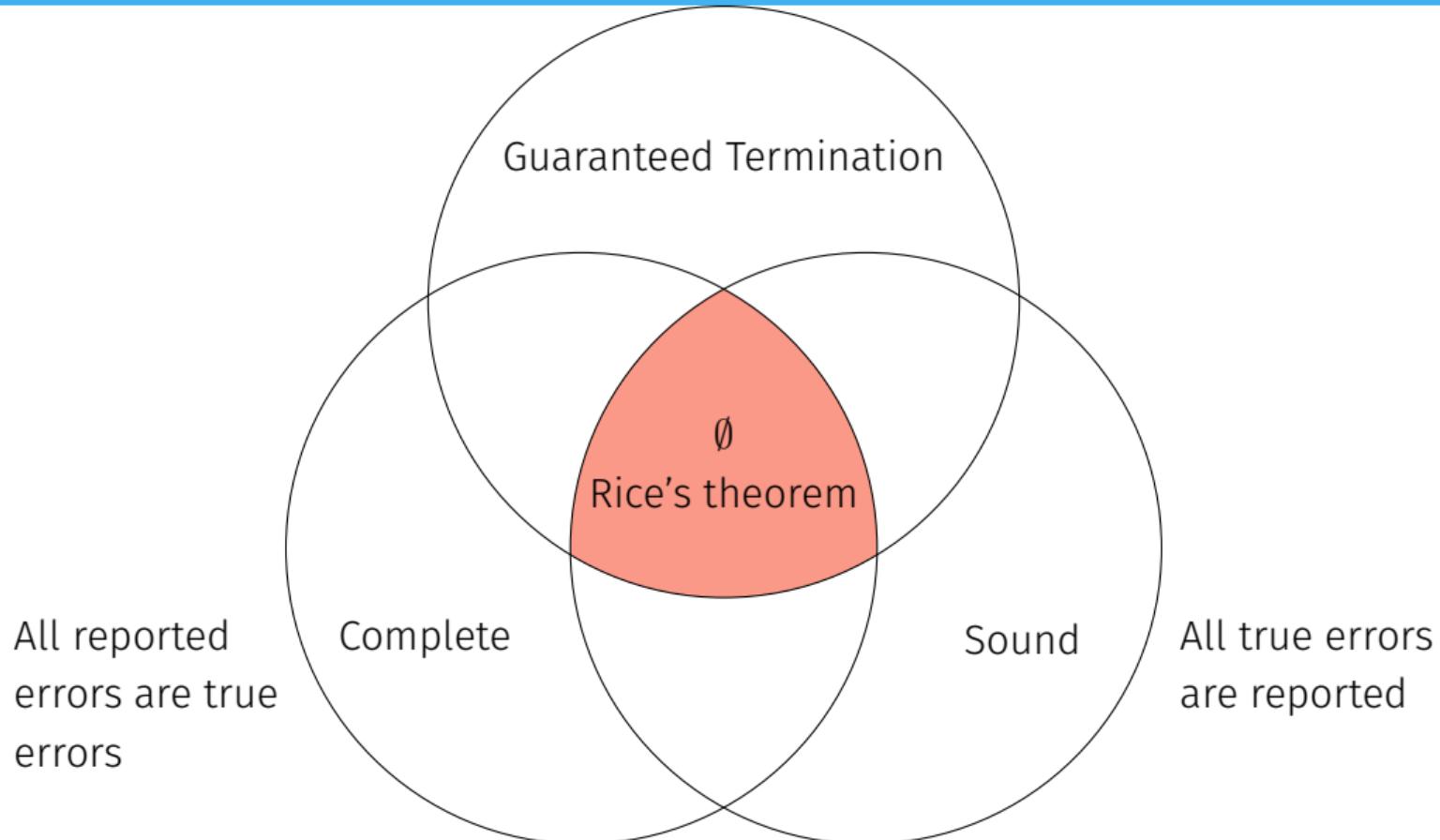
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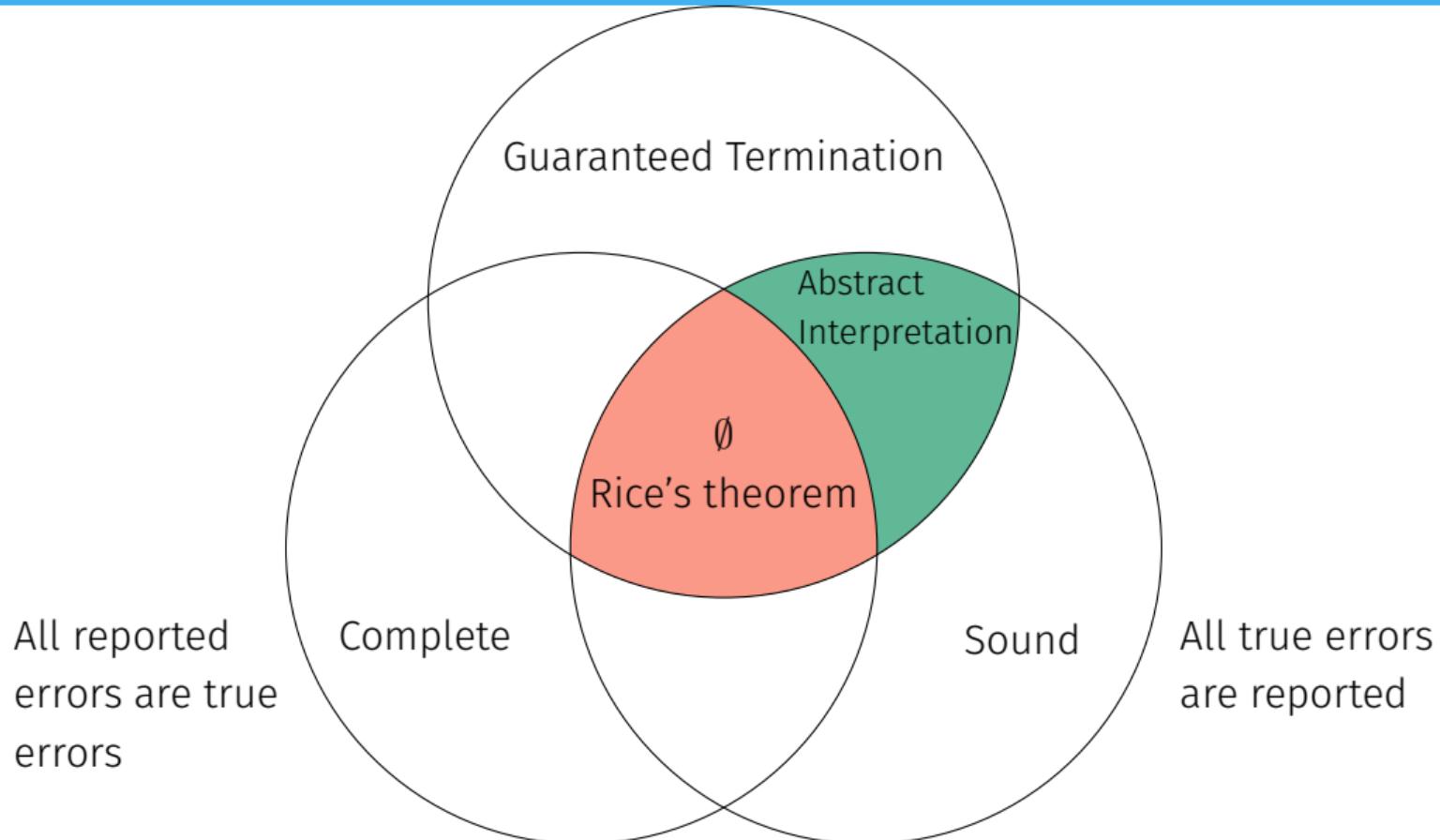
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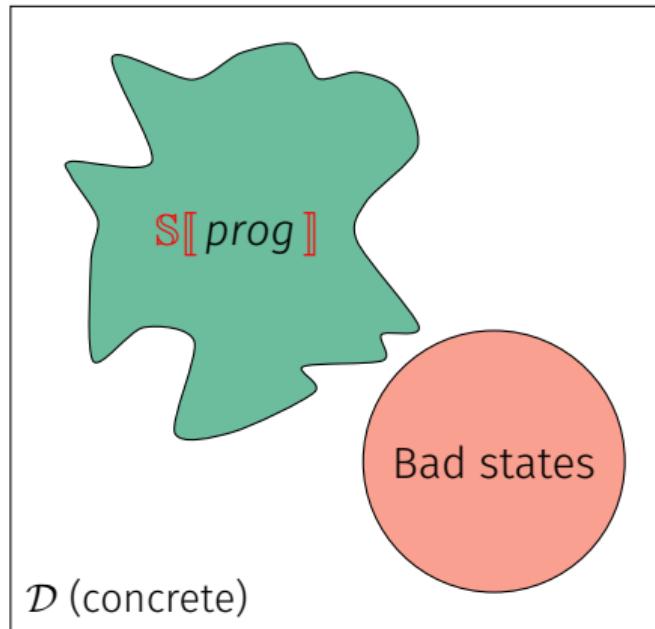
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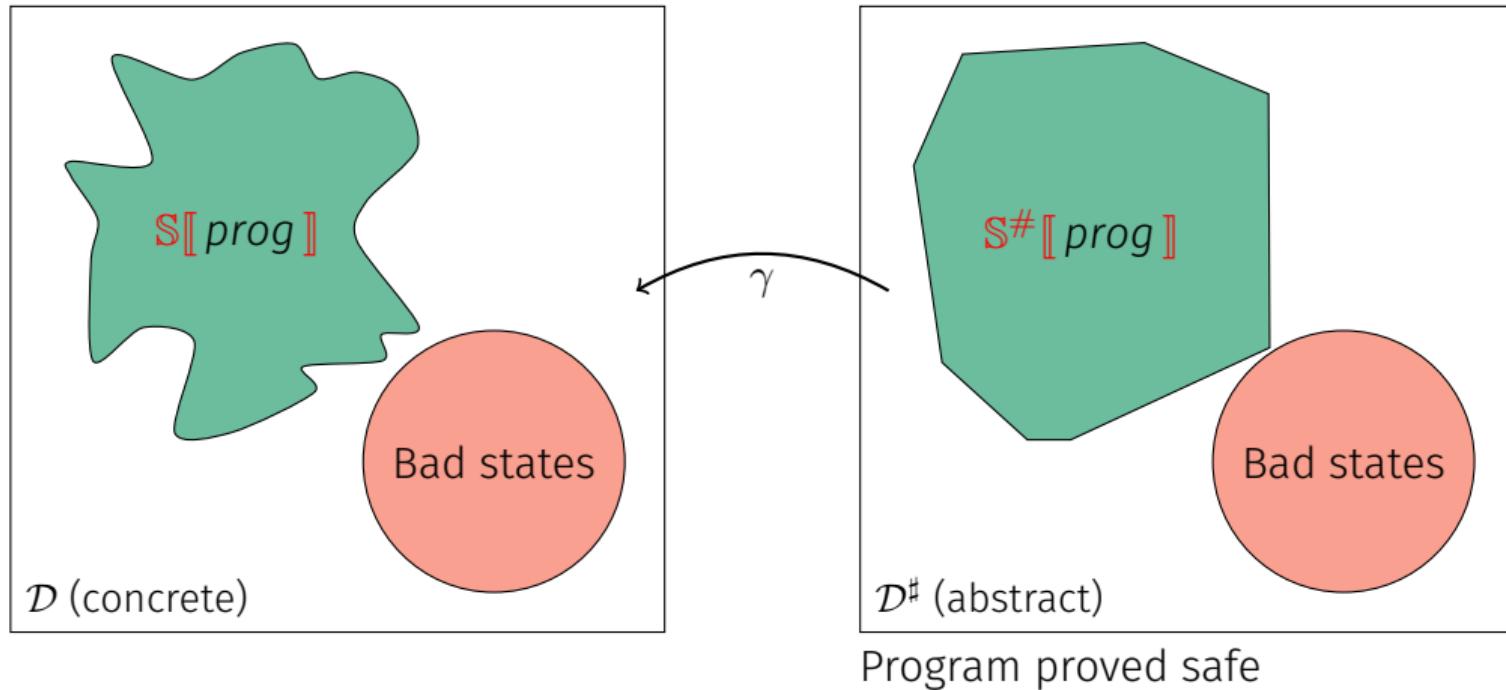


Abstract interpretation – the big picture



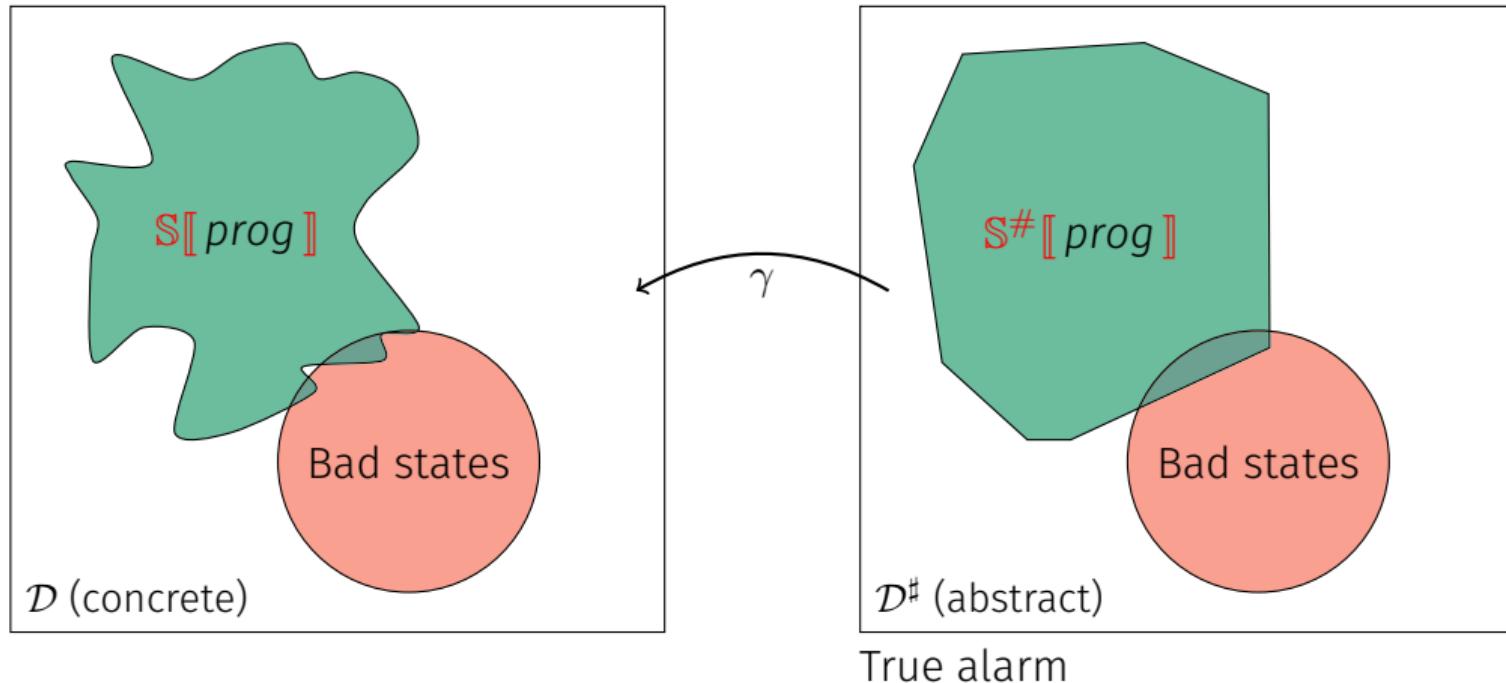
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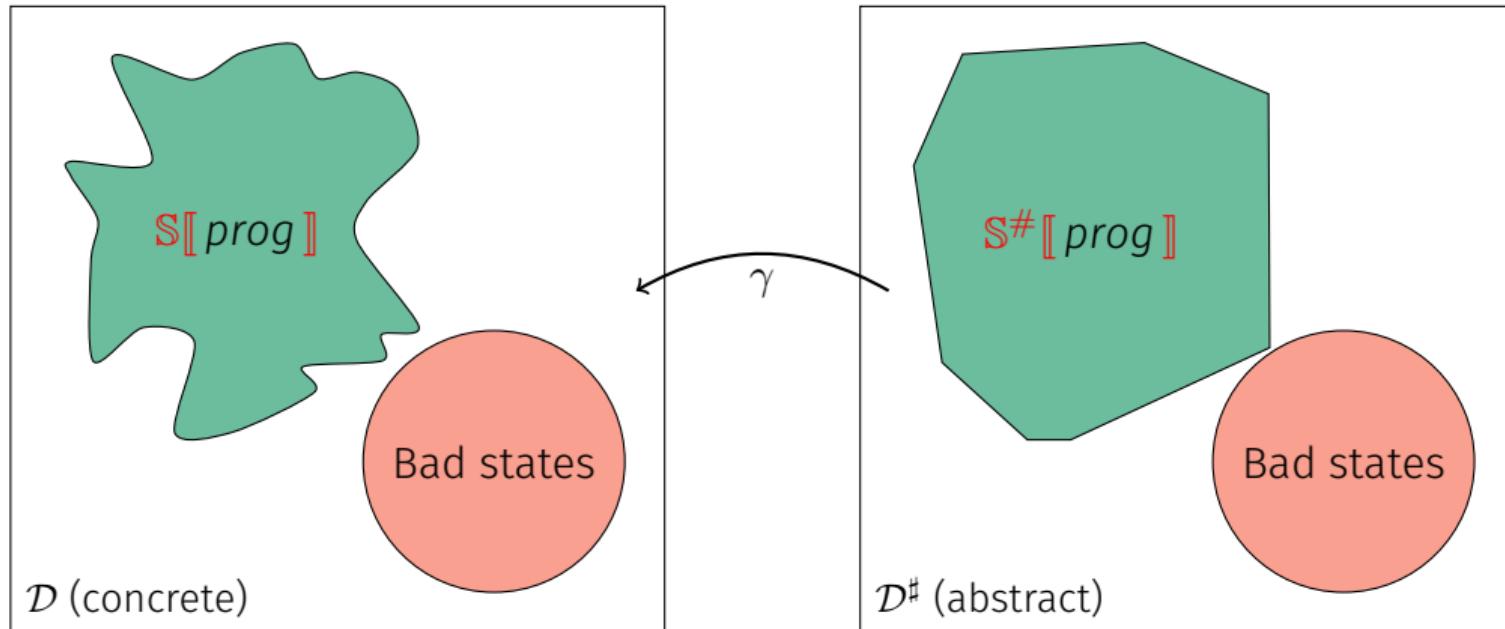
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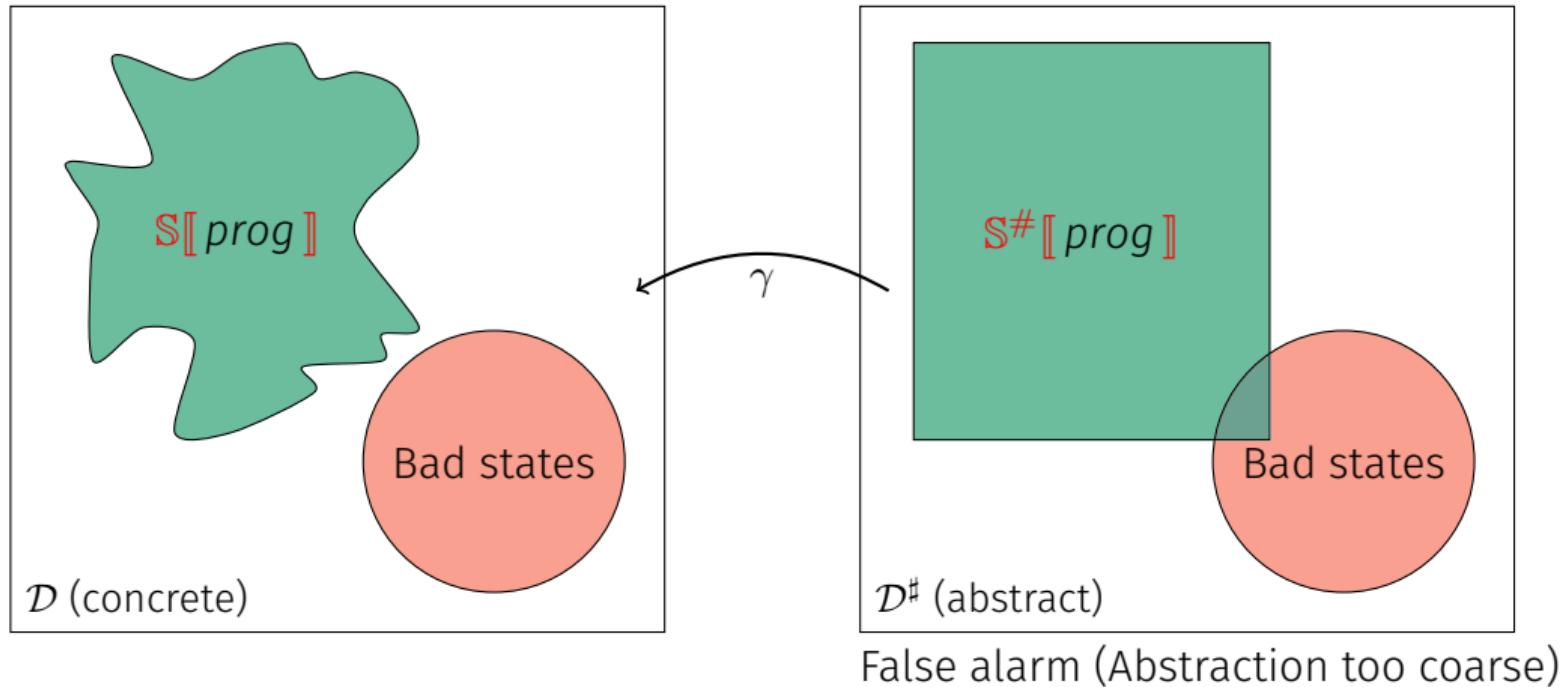
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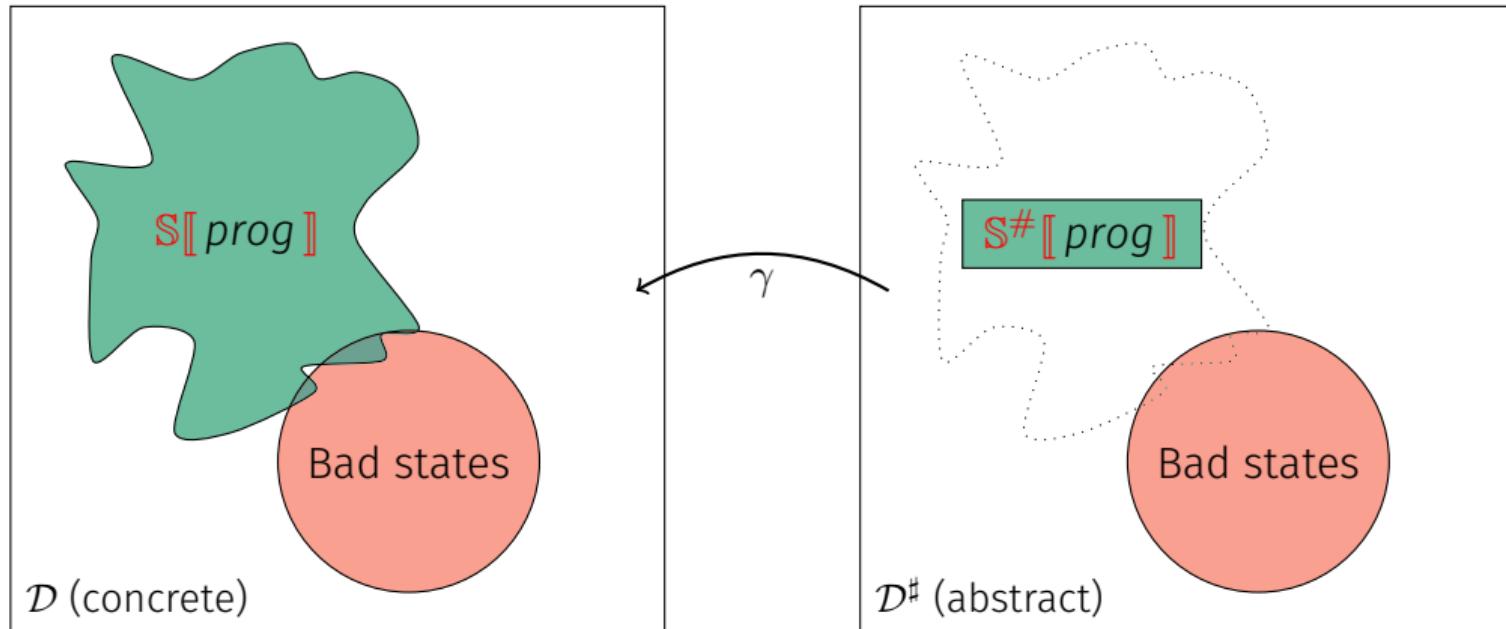
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Static analysis of critical software

Successfully applied to critical C software

- ▶ Astrée : Airbus A340, A380
- ▶ Frama-C : nuclear power plants

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How to analyze general software?

- ▶ New constructs: dynamic allocation, parallelism, ...
- ▶ New languages: Python, ...
- ▶ “Generic” static analyzers

Growing popularity

JavaScript #1, Python #2 on GitHub¹

¹<https://octoverse.github.com/#top-languages>

Dynamic programming languages

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New features

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- ▶ eval.

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Outline

- 1 Introduction
- 2 A Taste of Python
- 3 Analyzing Python Programs
- 4 Analyzing Python Programs with C Libraries
- 5 A Modern Compiler for the French Tax Code
- 6 Conclusion

A Taste of Python

No standard

- ▶ CPython is the reference
 - ⇒ manual inspection of the source code and handcrafted tests

Python's specificities

No standard

- ▶ CPython is the reference
⇒ manual inspection of the source code and handcrafted tests

Operator redefinition

- ▶ Calls, additions, attribute accesses
- ▶ Operators eventually call overloaded `__methods__`

Protected attributes

```
1 class Protected:  
2     def __init__(self, priv):  
3         self._priv = priv  
4     def __getattribute__(self, attr):  
5         if attr[0] == "_": raise AttributeError("...")  
6         return object.__getattribute__(self, attr)  
7     a = Protected(42)  
8 a._priv # AttributeError raised
```

Python's specificities (II)

Dual type system

- ▶ Nominal (classes, MRO)

Fspath (from standard library)

```
1 class Path:
2     def __fspath__(self): return 42
3
4 def fspath(p):
5     if isinstance(p, (str, bytes)):
6         return p
7     elif hasattr(p, "__fspath__"):
8         r = p.__fspath__()
9         if isinstance(r, (str, bytes)):
10            return r
11     raise TypeError
12
13 fspath("/dev" if random() else Path())
```

Barrett et al. "A Monotonic Superclass Linearization for Dylan". OOPSLA 1996

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Exceptions

Exceptions rather than specific values

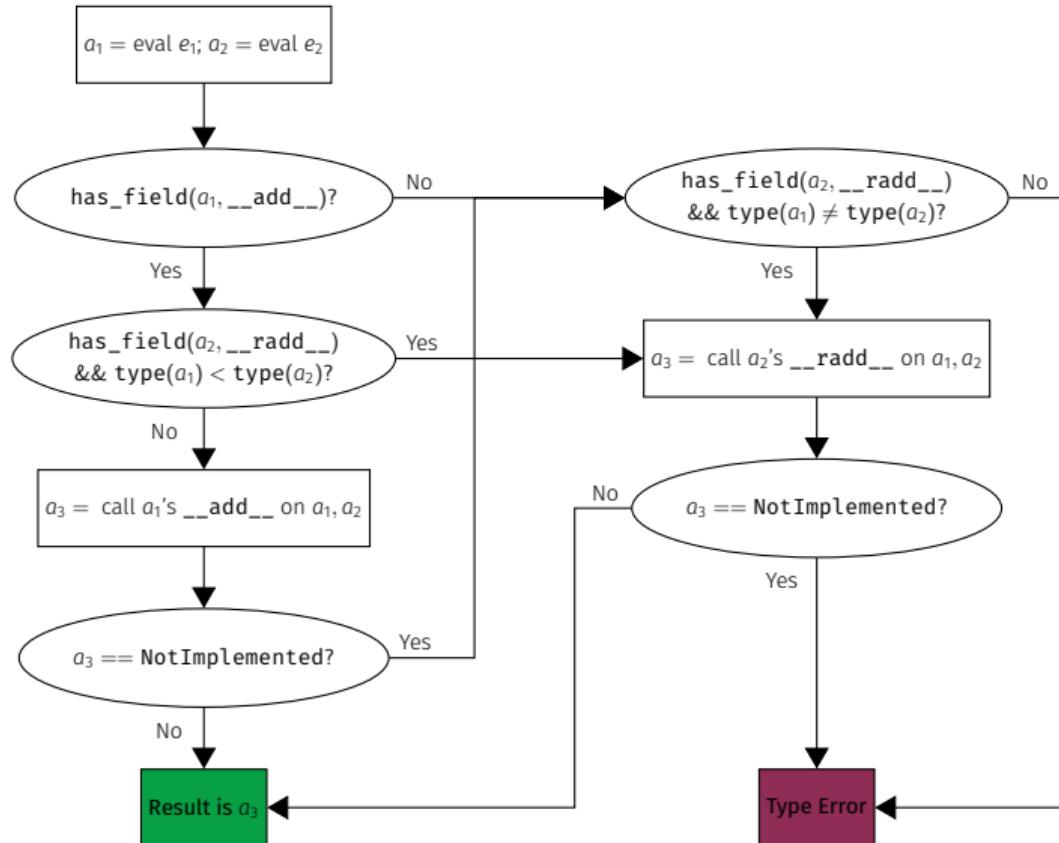
- ▶ `1 + "a" ~> TypeError`
- ▶ `l[len(l) + 1] ~> IndexError`

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Example Semantics – binary operators



Crazy Python

Custom infix operators

```
1 class Infix(object):
2     def __init__(self, func): self.func = func
3     def __or__(self, other): return self.func(other)
4     def __ror__(self, other): return Infix(lambda x: self.func(other, x))
5
6 instanceof = Infix(isinstance)
7 b = 5 |instanceof| int
8
9 @Infix
10 def padd(x, y):
11     print(f"{x} + {y} = {x + y}")
12     return x + y
13 c = 2 |padd| 3
```

Credits tomerfiliba.com/blog/Infix-Operators/

Analyzing Python Programs

Goal

Detect runtime errors: uncaught raised exceptions

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Detect runtime errors: uncaught raised exceptions

Supported constructs

Our analysis supports:

- ▶ Objects
- ▶ Exceptions
- ▶ Dynamic typing
- ▶ Introspection
- ▶ Permissive semantics
- ▶ Dynamic attributes
- ▶ Generators
- ▶ `super`
- ▶ Metaclasses

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Unsupported constructs

- ▶ Recursive functions
- ▶ `eval`
- ▶ Finalizers

Analysis | Domains required

Averaging numbers

```
1 def average(l):
2     m = 0
3     for i in range(len(l)):
4         m = m + l[i]
5     m = m // (i + 1)
6     return m
7
8 l = [randint(0, 20)
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Searching for a loop invariant (l. 4)

Environment abstraction

$$m \mapsto @_{\text{int}^{\#}} \quad i \mapsto @_{\text{int}^{\#}}$$

Proved safe?

- ▶ $m // (i+1)$
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Stateless domains: **list content**,

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Numeric abstraction (intervals)

$$m \in [0, +\infty) \quad \underline{\text{els}}(l) \in [0, 20] \quad i \in [0, +\infty)$$

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Stateless domains: list content, **list length**

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Numeric abstraction (polyhedra)

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Analysis | Domains required

Averaging tasks

```
1 class Task:
2     def __init__(self, weight):
3         if weight < 0: raise ValueError
4         self.weight = weight
5
6     def average(l):
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13    l = [Task(randint(0, 20))
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Searching for a loop invariant (l. 4)

Stateless domains: list content, list length

Environment abstraction

$$\begin{aligned}m &\mapsto @_{\text{int}\#}^{\sharp} \quad i \mapsto @_{\text{int}\#}^{\sharp} \quad \underline{\text{els}(l)} \mapsto @_{\text{Task}}^{\sharp} \\@_{\text{Task}}^{\sharp} \cdot \underline{\text{weight}} &\mapsto @_{\text{int}\#}^{\sharp}\end{aligned}$$

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Attributes abstraction

$$@_{\text{Task}}^{\sharp} \mapsto (\{\text{weight}\}, \emptyset)$$

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Conclusion

- ▶ Different domains depending on the precision
- ▶ Use of auxiliary variables (underlined)

Proved safe?

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Stateless domains: list content, list length

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$m \mapsto @_{Task}^{\#} \quad ; \quad @_{Task}^{\#}$

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Modular Open Platform for Static Analysis²

²Journault, Miné, Monat, and Ouadjaout. “Combinations of reusable abstract domains for a multilingual static analyzer”. VSTTE 2019.



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- ▶ One AST to analyze them all
 - 🚩 Multilanguage support
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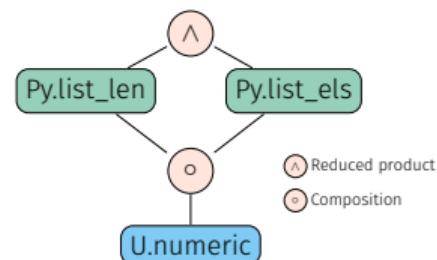


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Mopsa | Dynamic, semantic iterators with delegation

Universal.Iterators.Loops

Matches `while(...){...}`

Computes fixpoint using widening

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for(init; cond; incr) body
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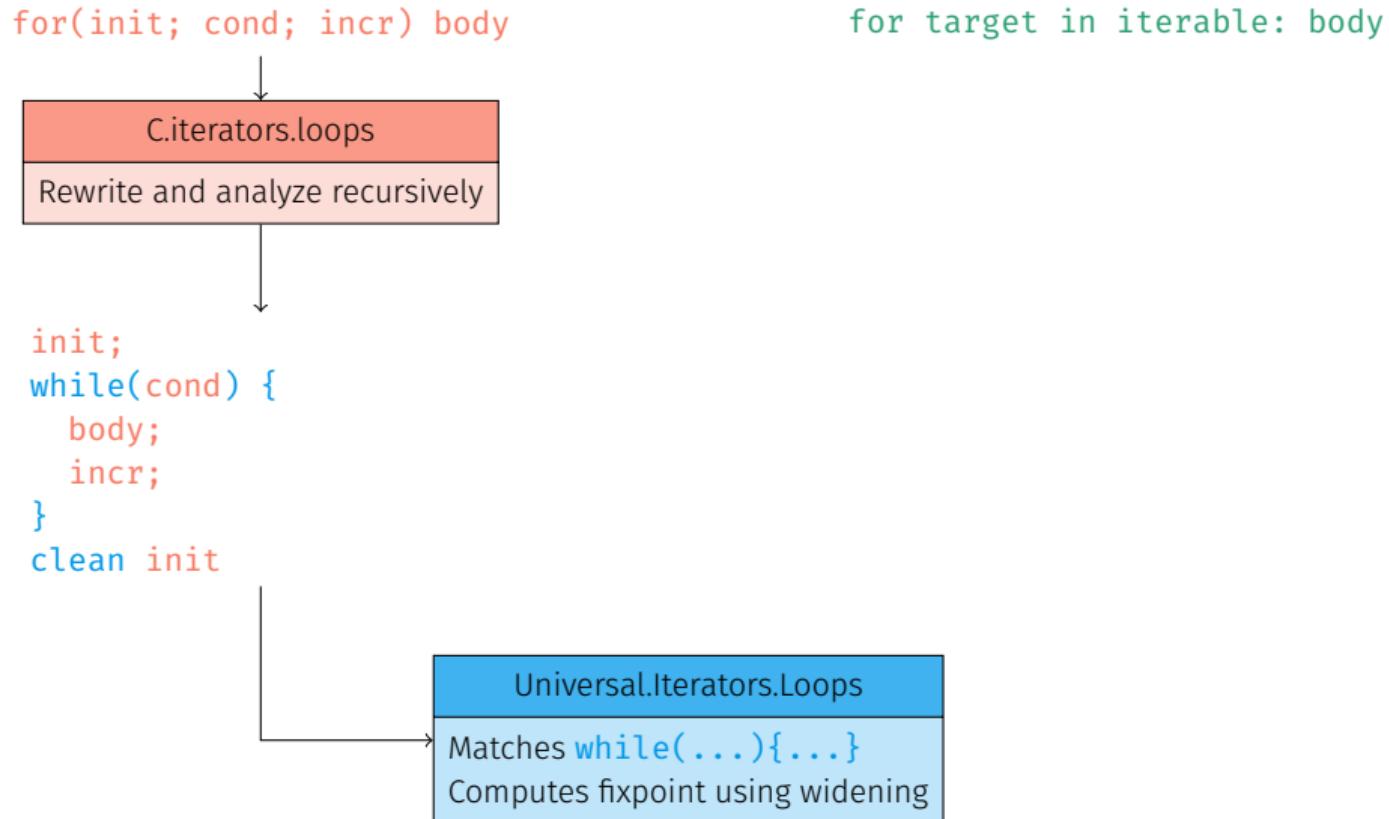
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init;  
while(cond) {  
    body;  
    incr;  
}  
clean init
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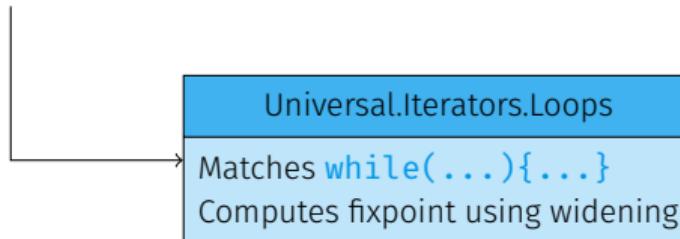
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for target in iterable: body
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Python.Desugar.Loops

- o Rewrite and analyze recursively
- o Optimize for some semantic cases



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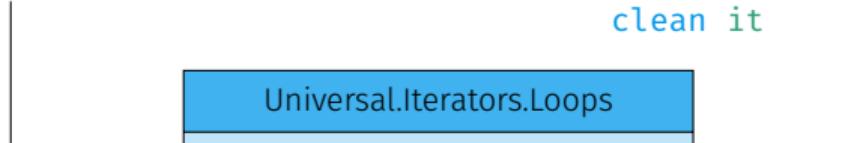
```
for target in iterable: body
```



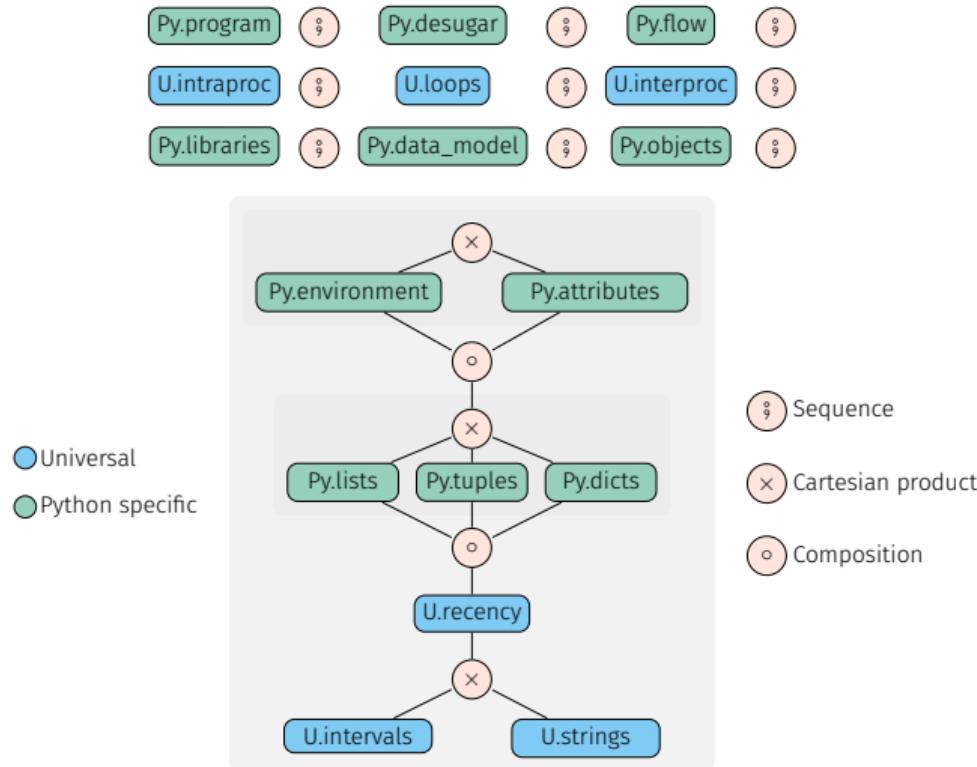
Python.Desugar.Loops

- o Rewrite and analyze recursively
- o Optimize for some semantic cases

```
it = iter(iterable)  
while(1) {  
    try: target = next(it)  
    except StopIteration: break  
    body  
}  
clean it
```



Definition of the Value Analysis



Comparison of the type and value analyses

Averaging tasks

```
1 class Task:  
2     def __init__(self, weight):  
3         if weight < 0: raise ValueError  
4         self.weight = weight  
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6     def average(l):  
7         m = 0  
8         for i in range(len(l)):  
9             m = m + l[i].weight  
10            m = m // (i + 1)  
11        return m  
12  
13    l = []  
14    for i in range(randint(5, 10)):  
15        l.append(Task(randint(0, 20)))  
16    m = average(l)
```

Type analysis

- **ValueError** (l. 3)

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- ▶ **IndexError** (l. 9)

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Non-relational value analysis

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Non-relational value analysis

IndexError (l. 9)

Relational value analysis

No alarm!

Comparison of the type and value analyses (II)

Name	LOC	Type Analysis					Non-relational Value Analysis				
		Time	Mem.	Exceptions detected			Time	Mem.	Exceptions detected		
		Type	Index	Key			Type	Index	Key		
nbbody.py	157	1.5s	3MB	0	22	1	5.7s	9MB	0	1	1
scimark.py	416	1.4s	12MB	1	1	0	3.4s	27MB	1	0	0
richards.py	426	13s	112MB	1	4	0	17s	149MB	1	2	0
unpack_seq.py	458	8.3s	7MB	0	0	0	9.4s	6MB	0	0	0
go.py	461	27s	345MB	33	20	0	2.0m	1.4GB	33	20	0
hexiom.py	674	1.1m	525MB	0	46	3	4.7m	3.2GB	0	21	3
regex_v8.py	1792	23s	18MB	0	2053	0	1.3m	56MB	0	145	0
processInput.py	1417	10s	64MB	7	7	1	12s	85MB	7	4	1
choose.py	2562	1.1m	1.6GB	12	22	7	2.9m	3.7GB	12	13	7
Total	9294	4.0m	2.8GB	59	2214	12	13m	9.1GB	59	228	12

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scimark.py	416	1.4s	—	—	—	1.4s	—	0	0		
richards.py	426	13s	—	—	—	13s	—	2	0		
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The non-relational value analysis

- ▶ does not remove false type alarms
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- ▶ is $\simeq 3\times$ costlier

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Heuristic packing and relational analyses

- ▶ Static packing, using function's scope
- ▶ Rules out all 145 alarms of `regex_v8.py` (1792 LOC) at $2.5\times$ cost

Analyzing Python Programs with C Libraries

Combining C and Python – motivation

One in five of the top 200 Python libraries contains C code

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- ▶ Different runtime-errors (exceptions in Python)
- ▶ Garbage collection

Combining C and Python – example

counter.c

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1 typedef struct {
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1 from counter import Counter
2 from random import randrange
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How to analyze multilanguage programs?

Type annotations

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class Counter:  
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Type annotations

Rewrite into Python code

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```

- ▶ No integer wrap-around in Python
- ▶ Some effects can't be written in pure Python (e.g., read-only attributes)

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Rewrite into Python code

Drawbacks of the current approaches

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- ▶ Analyze both the C and Python sources

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Our approach

- ▶ Analyze both the C and Python sources
- ▶ Switch from one language to the other just as the program does
- ▶ Reuse previous analyses of C and Python
- ▶ Detect runtime errors in Python, in C, and at the boundary

Analysis result

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<pre>1 typedef struct { 2 PyObject_HEAD; 3 int count; 4 } Counter; 5 6 static PyObject* 7 CounterIncr(Counter *self, 13: self->count += i; 8 { 9 int i = 1; 10 if(!PyArg_ParseTuple(a 11 return NULL; 12 13 self->count += i; 14 Py_RETURN_NONE; 15 } 16 17 static PyObject* 18 CounterGet(Counter *self) 6: c.incr(2**p-1) 19 { 20 return Py_BuildValue("U"); 21 }</pre>	<pre>1 from counter import Counter 2 from random import randrange 3 4 △ Check #430: 5 ./counter.c: In function 'CounterIncr': 6 ./counter.c:13.2-18: warning: Integer overflow 7 8 Callstack: 9 from count.py:8.0-8: CounterIncr 10 11 ('self->count + i)' has value [0,2147483648] that is larger 12 than the range of 'signed int' = [-2147483648,2147483647] 13 14 Callstack: 15 from count.py:8.0-8: CounterIncr 16 17 X Check #506: 18 count.py: In function 'PyErr_SetString': 19 count.py:6.0-14: error: OverflowError exception 20 21 Callstack: 22 from ./counter.c:17.6-38::convert_single[0]: PyParseTuple_int 23 from count.py:7.0-14: CounterIncr 24 25 +1 other callstack</pre>

High-level idea

Difficulty: shared memory

- ▶ Each language may change the memory state, and has a different view of it
- ▶ Synchronization? We could perform a full state translation, but
 - the cost would be high in the analysis
 - some abstractions can be shared between Python and C

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State separation \rightsquigarrow reduced synchronization

- ▶ Observation: structures are directly dereferenceable by one language only
- ▶ Switch to other language otherwise (`c.incr()` \rightsquigarrow `self->count += 1`)
Additional hypothesis: C accesses to Python objects through the API
- ▶ Synchronization: only when objects change language for the first time
- ▶ Mopsa supports shared abstractions

Concrete definition

- ▶ Builds upon the Python and C semantics

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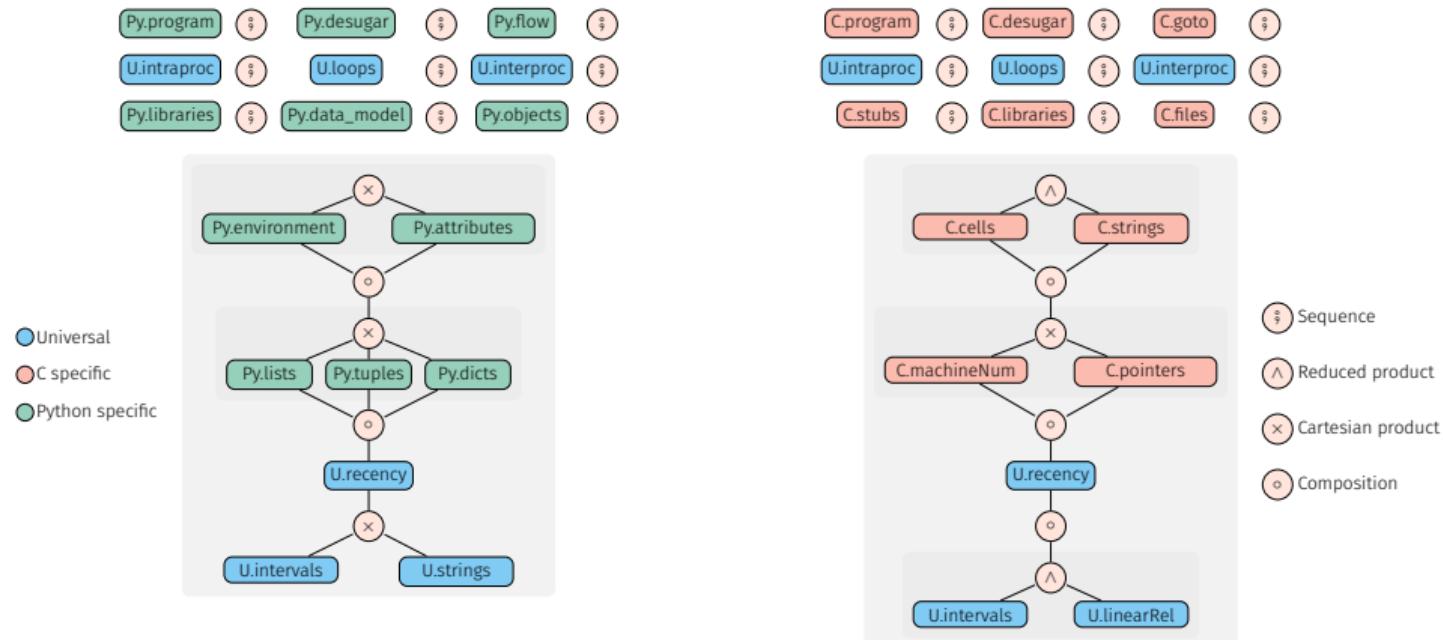
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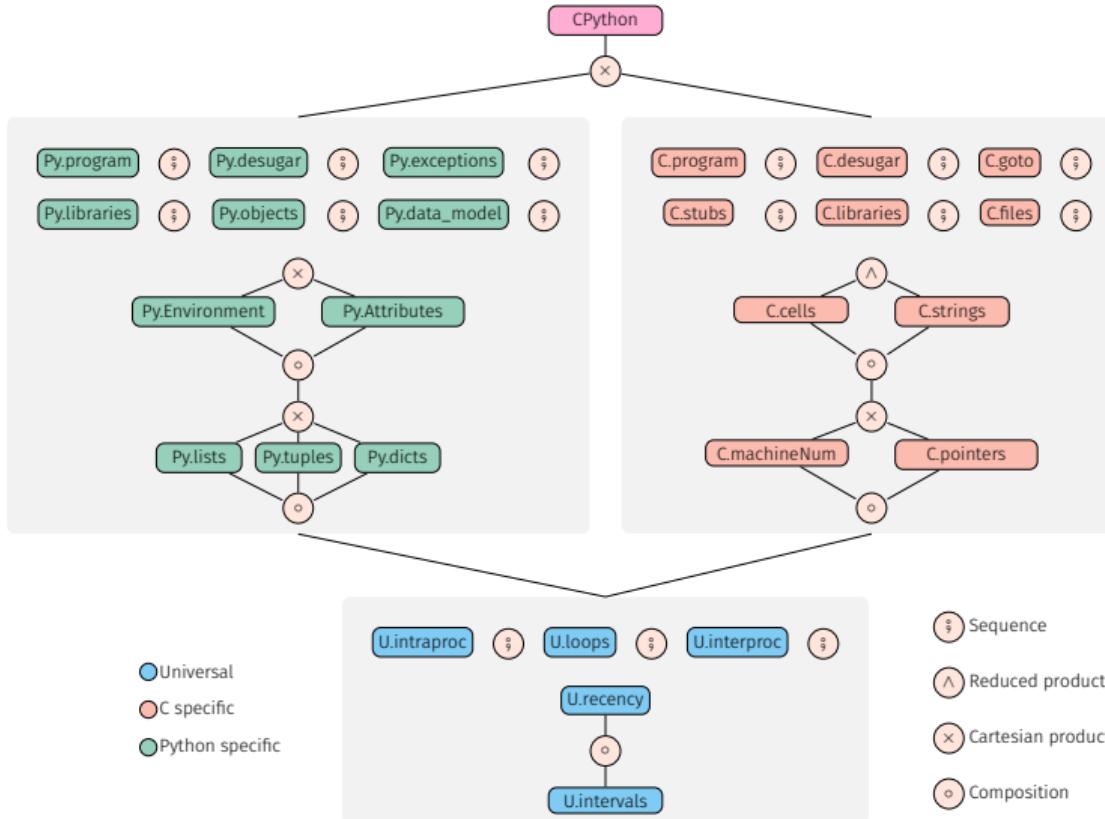
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- ▶ Garbage collection not handled
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- ▶ Manual modelization from CPython's source code

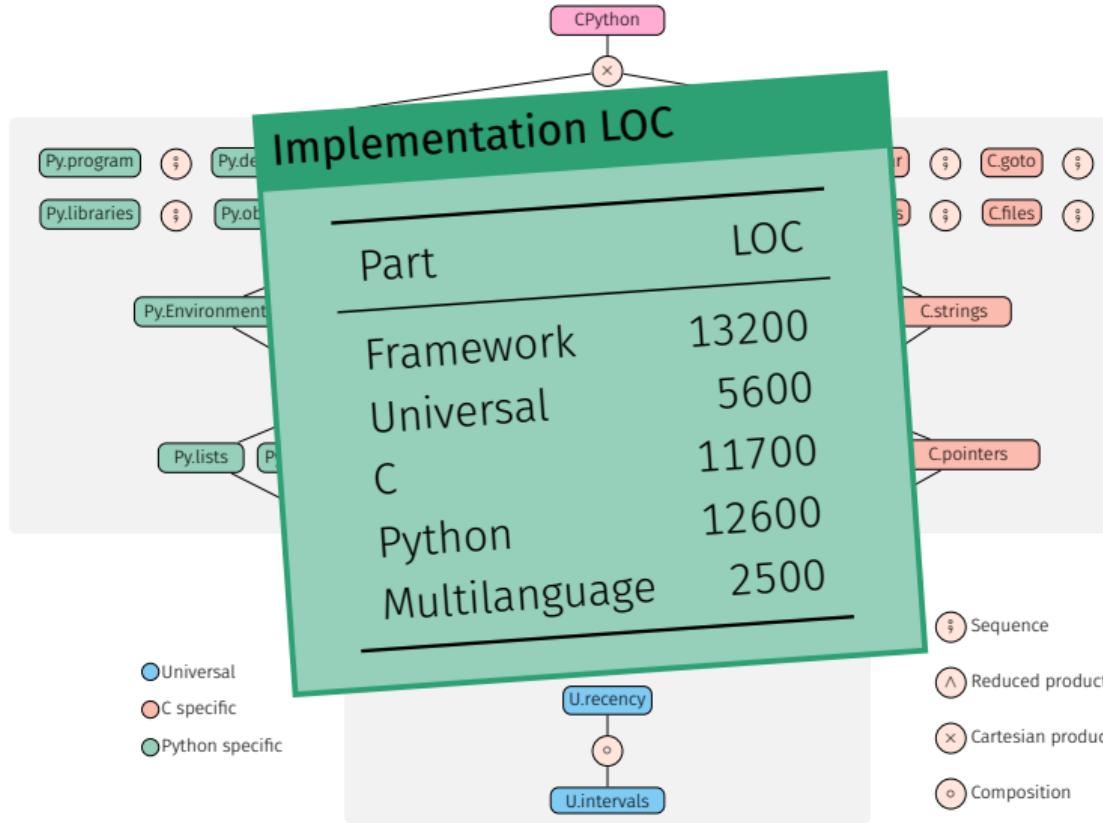
From distinct Python and C analyses...



From distinct Python and C analyses... to a multilanguage analysis!



From distinct Python and C analyses... to a multilanguage analysis!



Benchmarks

Corpus selection

- ▶ Popular, real-world libraries available on GitHub, averaging 412 stars.
- ▶ Whole-program analysis: we use the tests provided by the libraries.

Library	C + Py.	Loc	Tests	⌚/test	# proved checks # checks %	# checks
noise		1397	15/15	1.2s	99.7%	(6690)
cdistance		2345	28/28	4.1s	98.0%	(13716)
llist		4515	167/194	1.5s	98.8%	(36255)
ahocorasick		4877	46/92	1.2s	96.7%	(6722)
levenshtein		5798	17/17	5.3s	84.6%	(4825)
bitarray		5841	159/216	1.6s	94.9%	(25566)

Contributions around the static analysis of Python programs

Python's semantics

$$\text{Python} \rightsquigarrow \mathbb{S}_{py}[\cdot]$$

- ▶ Reverse-engineering CPython (160kLoc C)
- ▶ Backlinks to source code (auditability)
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Python's analyses

$$\mathbb{S}_{py}[\cdot] \rightsquigarrow \mathbb{S}_{py}^{\#}[\cdot]$$

- ▶ Type and value analyses
- ▶ Combining numerous abstractions
- ▶ Analysis of real programs

Contributions around the static analysis of Python programs

Python's semantics

$$\text{Python} \rightsquigarrow \mathbb{S}_{py}[\cdot]$$

- ▶ Reverse-engineering CPython (160kLoc C)
- ▶ Backlinks to source code (auditability)
- ▶ On-paper formalization ($\simeq 44$ pages)

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- ▶ First real multilanguage analysis
- ▶ Reuses off-the-shelf Python and C analyses
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Implementation into Mopsa

- ▶ Open-source analyzer for C and Python
- ▶ Factors abstractions between languages
- ▶ Sharing between abstractions

A Modern Compiler for the French Tax Code

Research field: formal methods

⇒ Improve confidence in software.

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Personal methodology

Constant back and forth between theory and practice

- 1 Find interesting bugs, properties or systems to study (GitHub, ...)
- 2 Theoretical study and solution
- 3 Implementation and experimental validation (on 1)

Legal implementations

French income tax

- ▶ 38M households, 75Md€ of income
- ▶ Made public in April 2016 : \simeq 92kLoc M, custom language
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Trusting the computation?

- ▶ Reproducibility of the computation?
- ▶ Accurate simulation of tax reforms?
- ▶ Compliance with the law, acting as specification?

Example M code

Variable declaration

```
IRNETBIS : calculee primrest = 0 : "IRNET avant bidouille du 8ZI" ;  
8ZI : "Impot net apres depart a l'etrange (non residents)" ;
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Example M code

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IRNETBIS : calculee primrest = 0 : "IRNET avant bidouille du 8ZI" ;
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```

Computation rule

```
rule 221220:
application : iliad ;
IRNETBIS = max(0, IRNETTER -
    PIR * positif(SEUIL_12 - IRNETTER + PIR)
    * positif(SEUIL_12 - PIR)
    * positif_ou_nul(IRNETTER - SEUIL_12));
```

M, briefly

The core of M: **arithmetic expressions** assigned to variables.

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- ▶ Small, unrollable loops
- ▶ Use of floating-point numbers, booleans are zero and one
- ▶ `undef` value

A formal semantics for M

We reverse-engineered the semantics:

- ▶ At first, using the online simulator³
- ▶ Later, using the private tests DGFIP sent us ([August 7, 2019](#))

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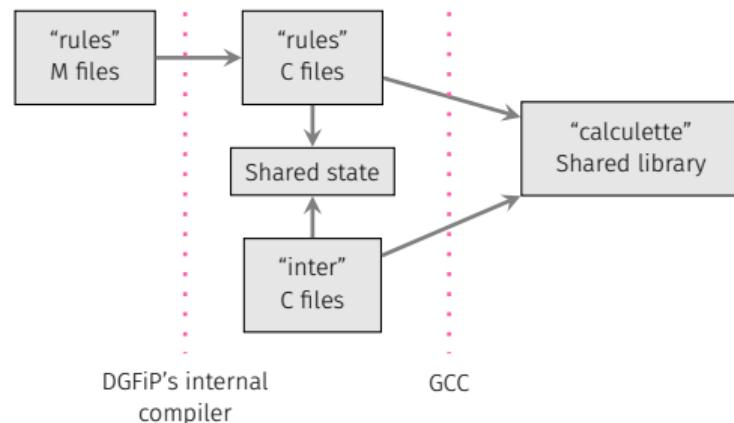
The **undef** value

- ▶ Used for: default inputs, runtime errors & missing cases in inline conditionals
- ▶ Fun facts: $f + \text{undef} = f$, $f \div 0 = 0$, $x[|x| + 1] = \text{undef}$, $x[-1] = 0$...

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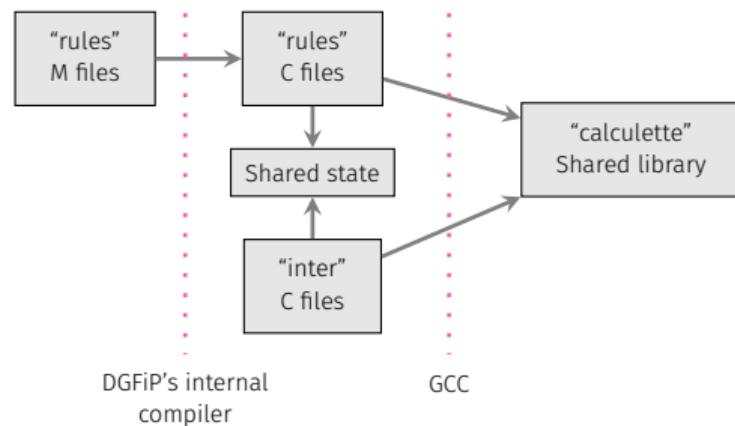
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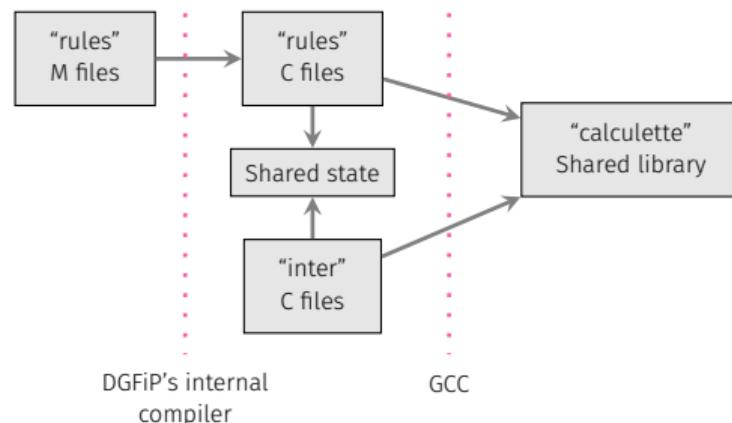


"inter" files

35kLoc of C to bypass M's lack of functions.

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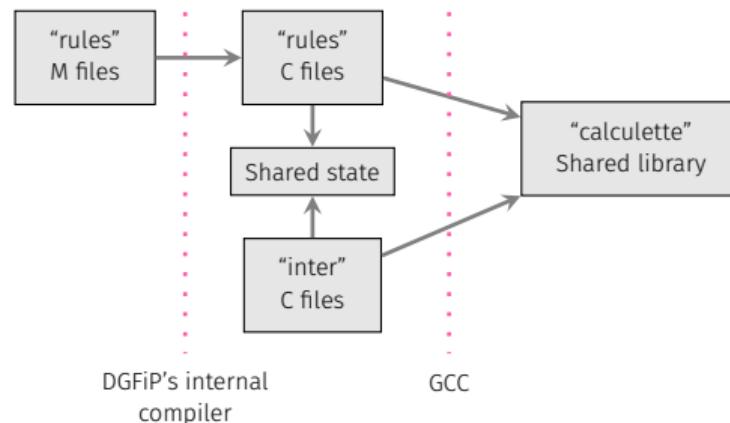
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DSLs to the rescue! Introducing M++

- ▶ High-level, no mutable state under the hood
- ▶ Tailored for the needs of the "inter" files and DGFiP devs
- ▶ 6,000 lines of "inter" C code ⇒ 100 lines of M++

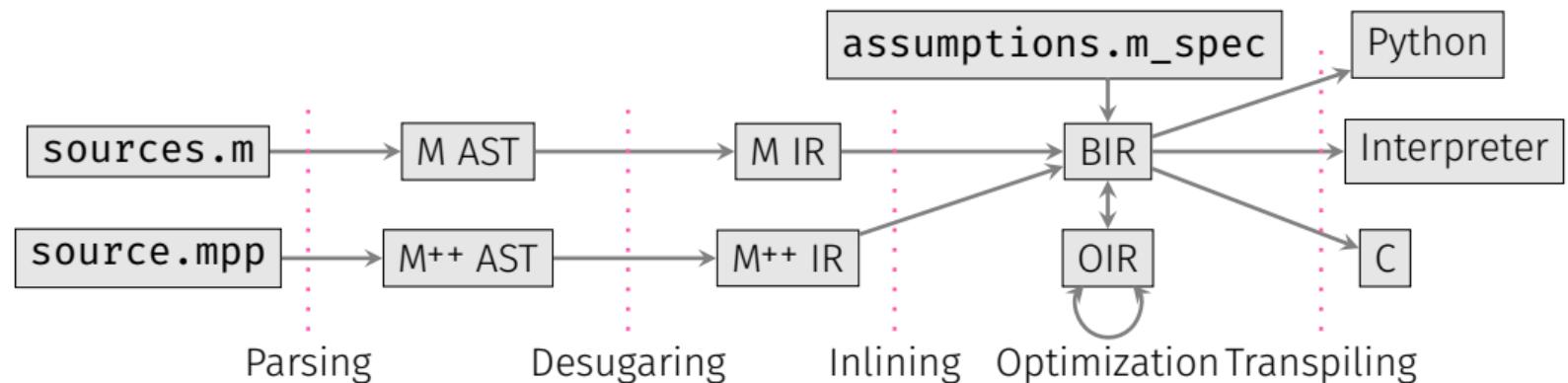
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MLANG: written in OCaml, 10k lines of code

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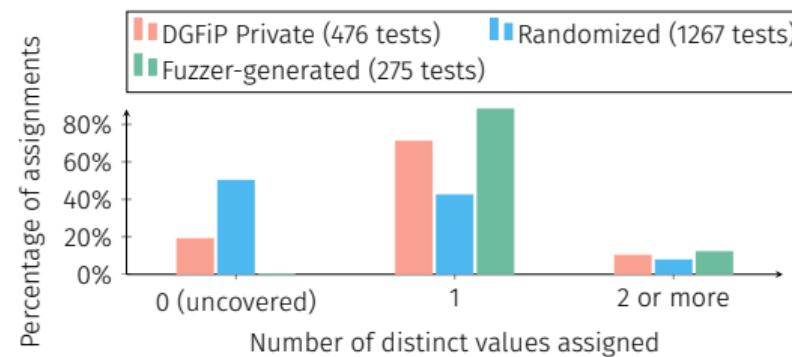
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- ▶ Global value numbering
- ▶ Dead code elimination
- ▶ Partial evaluation
- ▶ Dataflow defined-ness analysis

Code optimization

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Spec. name	# inputs	# outputs	# instructions	% reduction
All	2,459	10,411	129,683	80.2%
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Contributions around the French tax code

Component	Published by DGFiP?	Contributions
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“inter” code (C)	no	DSL M++ (6kLoc C \rightsquigarrow 100 M++)
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Interacting with DGFIP

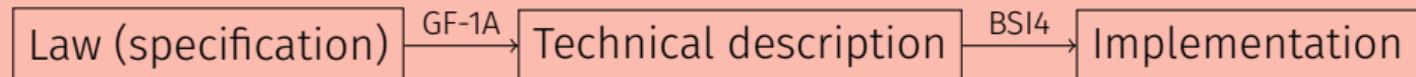
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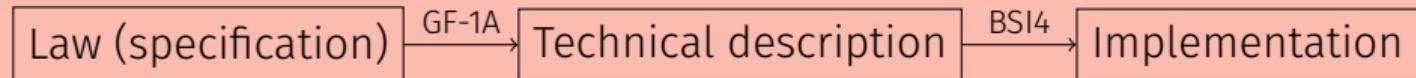
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“inter” code (C)	no	DCL-M ($\rightsquigarrow \mu\text{M}$)
M compiler		optimizations error coverage
Tests		Ongoing work to bring MLANG at DGFIP. ▶ 30-day mission between January and August ▶ Supervision of 3 developers (2 OCamlPro, 1 DGFIP)
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Merigoux, Raphaël Monat, and Protzenko. “A Modern Compiler for the French Tax Code”. Compiler Construction (CC) 2021

Does the implementation comply with the law?



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- ▶ No structural correspondance
- ▶ 2019~~2020 : 30% of 90kLoc M changed

Does the implementation comply with the law?

Catala, another DSL to the rescue

Article D521-1 du code de la sécurité sociale

I - Pour l'application de l'article L. 521-1 , le montant des allocations familiales et de la majoration pour âge prévue à l'article L. 521-3 est défini selon le barème suivant :

1° Lorsque le ménage ou la personne a disposé d'un montant de ressources inférieur ou égal au plafond défini au I de l'article D. 521-3, les taux servant au calcul des allocations familiales sont fixés, en pourcentage de la base mensuelle prévue à l'article L. 551-1, à :

a) 32 % pour le deuxième enfant à charge ;

```
```catala
champ d'application AllocationsFamiliales :
 définition montant_initial_base_deuxième_enfant sous condition
 ressources_ménage ≤ plafond_I_d521_3
 conséquence égal à
 si nombre de enfants_à_charge_droit_ouvert_prestation_familiale ≥ 2
 alors prestations_familiales.base_mensuelle × € 32 %
 sinon 0 €
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```

- ▶ Literal programming
- ▶ Default logic
- ▶ Participation to ongoing development

Conclusion

Summary of the contributions

Static analysis of Python programs using C libraries

- ▶ Ouadjaout and Miné (LIP6, Sorbonne Université)
- ▶ SAS'21, ECOOP'20, VSTTE'19 (invited), SOAP@PLDI'20 (award), JFLA'21 (fr, tool)
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A modern compiler for the French tax code

- ▶ Merigoux (Prosecco, Inria Paris) et Protzenko (Microsoft Research)
- ▶ CC'21, JFLA'20 (fr), JFLA'21 (fr, tool)
- ▶ Mlang (GPL v3, 10kLoc OCaml), main contibutor since May 2019
- ▶ Ongoing transfer work
 - 30 days mission between January and August
 - Supervision of 3 developers (2 OCamlPro, 1 DGFiP)

Current state of static analysis tools

- ▶ Astrée: sound analysis of specific critical systems
 - ▶ Infer: bug detector for general programs
- ⇒ Unify approaches to ensure a massive adoption by developers

Future research directions

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- ⇒ Unify approaches to ensure a massive adoption by developers

Precise, sound and efficient static analyses for general programs

- 1 Formalization and analysis of concrete semantics  $\rightsquigarrow \mathbb{S}_{py}[\cdot] \rightsquigarrow \mathbb{S}_{py}^{\#}[\cdot]$
- 2 Make static analysis more usable
- 3 Formal methods for legal code

Formal methods for real-world systems: study of two cases

Questions

Raphaël Monat

LIP, ENS de Lyon
28 April 2022

rmonat.fr

