

# From Python to the French Tax Code: Applying Formal Methods on Real Systems

Raphaël Monat

SyCoMoRES team

`rmonat.fr`

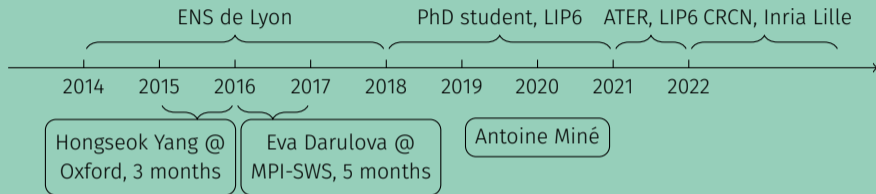
DI Seminar  
22 March 2023



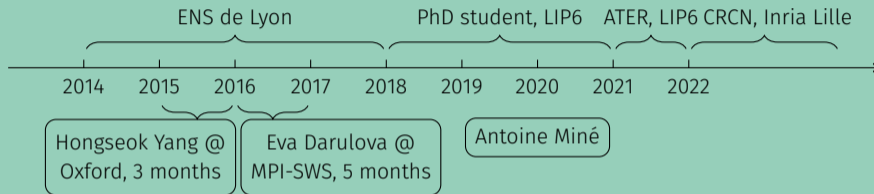
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## Curriculum



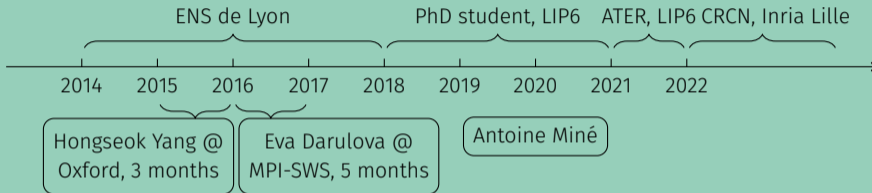
## Curriculum



## Research field: formal methods

⇒ Improve confidence in software.

## Curriculum



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Means

- ▶ Theory: formal definition and reasoning over systems
- ▶ Practice: software development

## Personal methodology

Constant back and forth between theory and practice

- 1 Find interesting bugs, properties or systems to study (GitHub, ...)
- 2 Theoretical study and solution
- 3 Implementation and experimental validation (on 1)

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- ▶ Python programs using C libraries  $\rightsquigarrow$  static analysis
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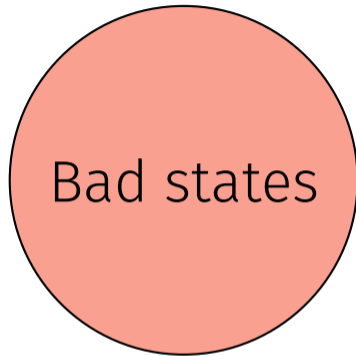
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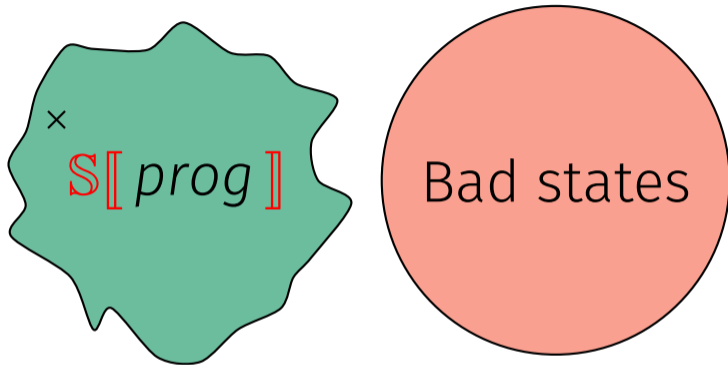
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- ▶ Python programs using C libraries  $\rightsquigarrow$  static analysis
  - Abdelraouf Ouadjaout (LIP6)
  - Antoine Miné (LIP6)
- ▶ Implementation of the French tax code  $\rightsquigarrow$  compiler, modernization
  - Denis Merigoux (Inria Prosecco)
  - Jonathan Protzenko (MSR)

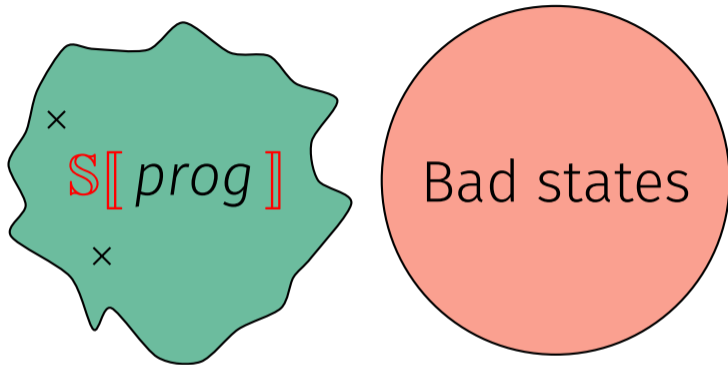




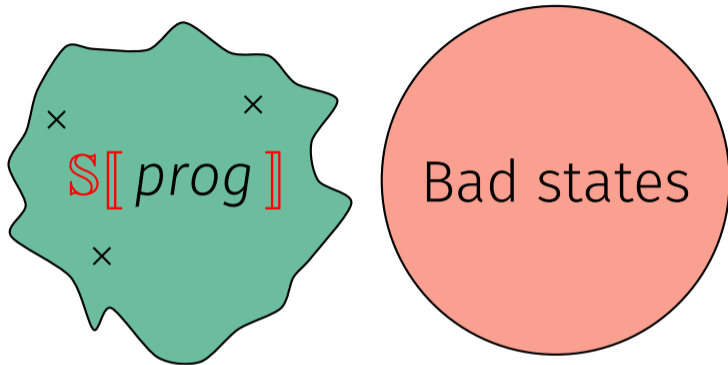




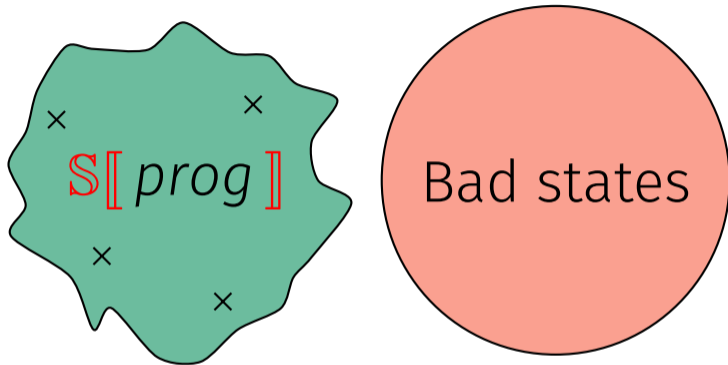
Cheap approach: test *prog*.



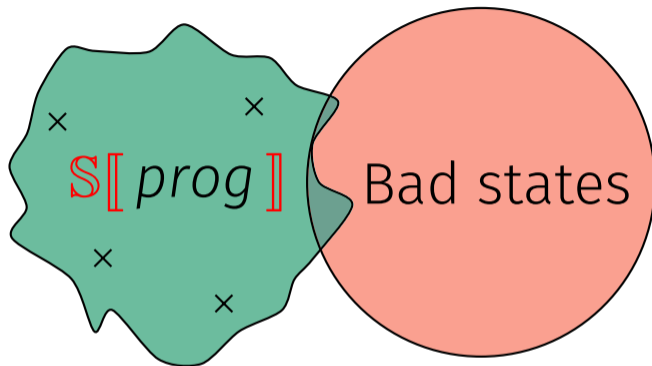
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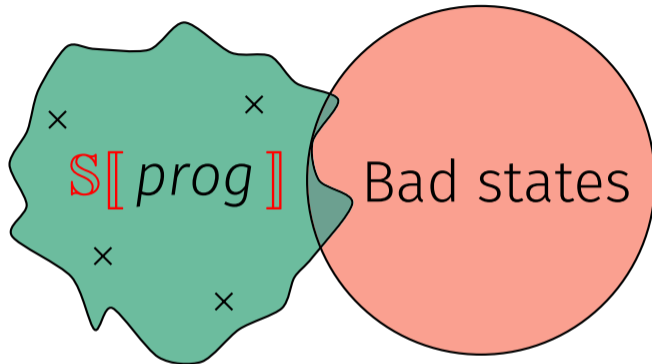
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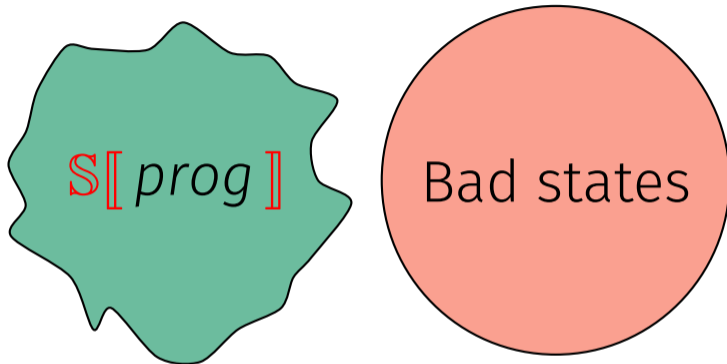
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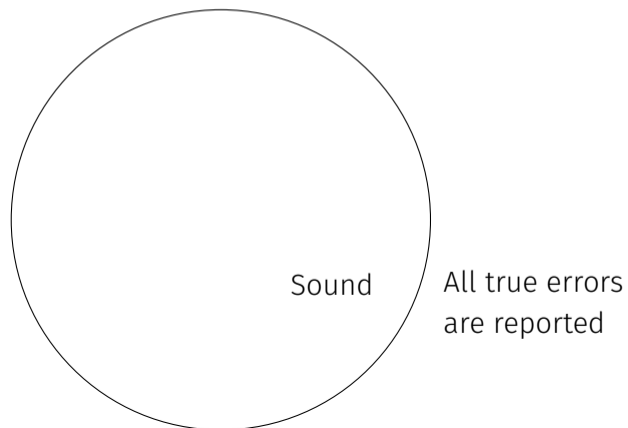


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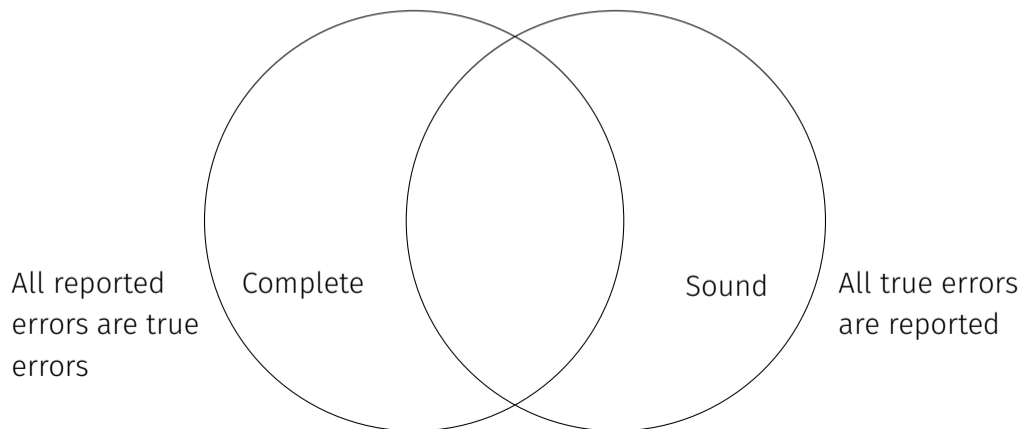
Would there be a way to automatically prove programs correct?



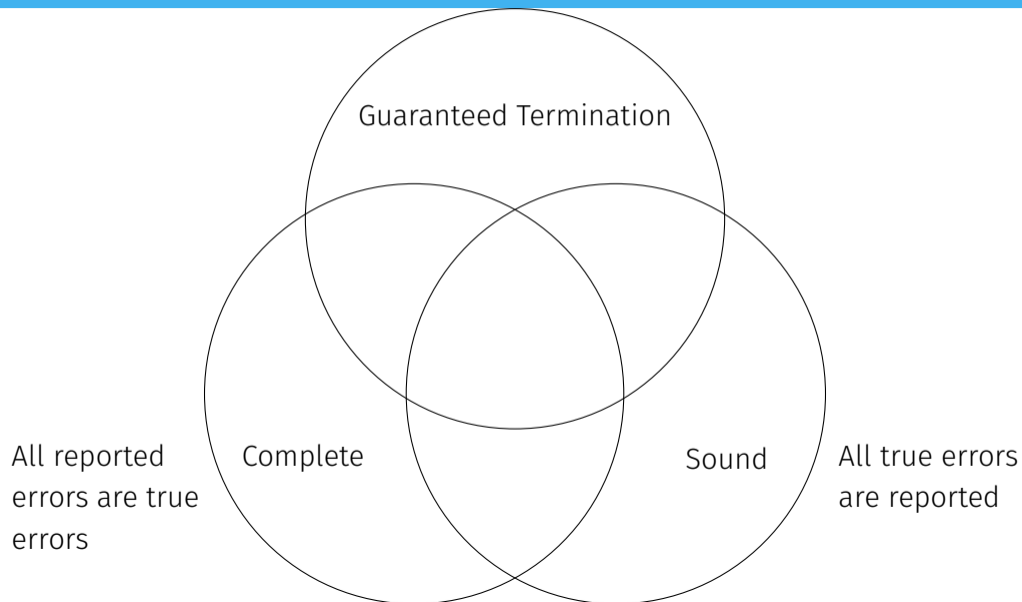
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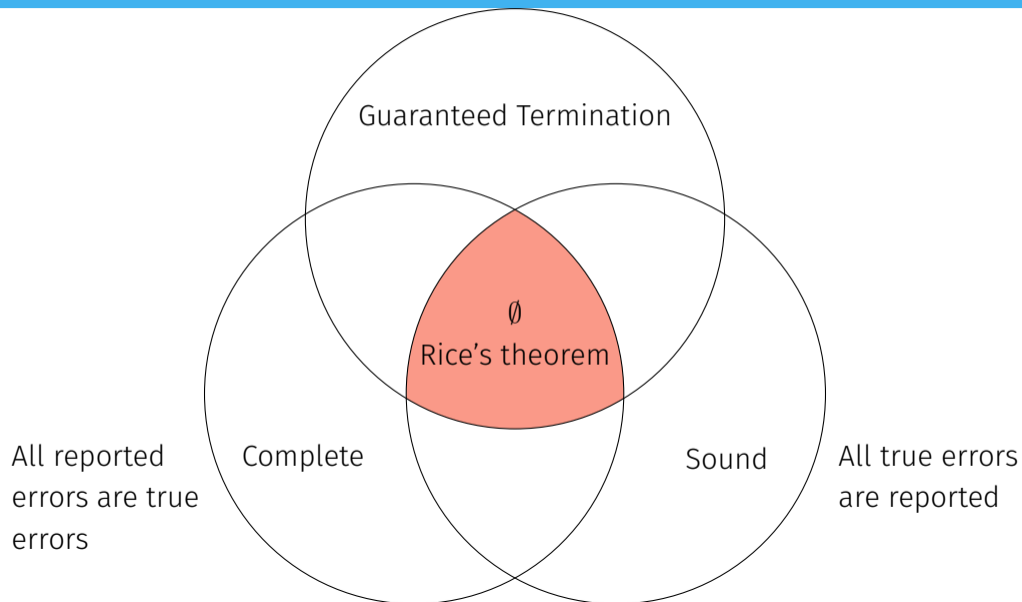
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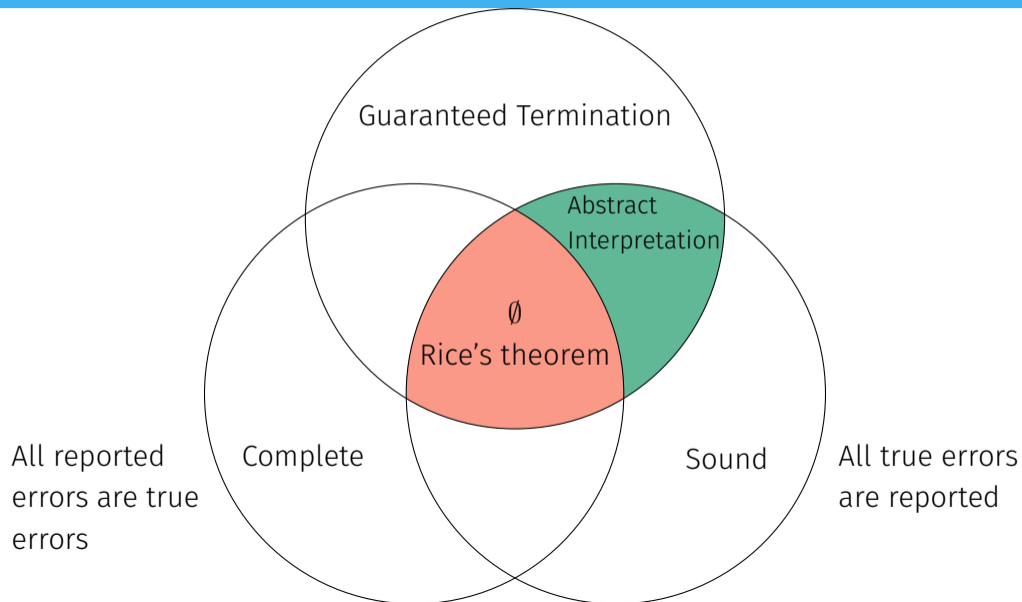
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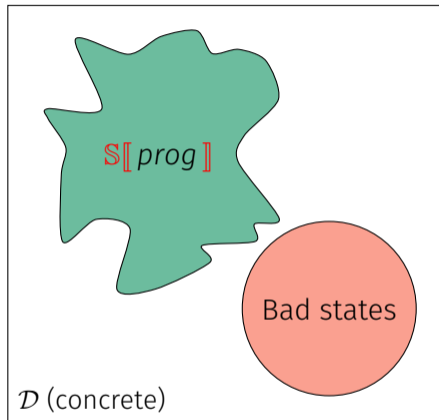
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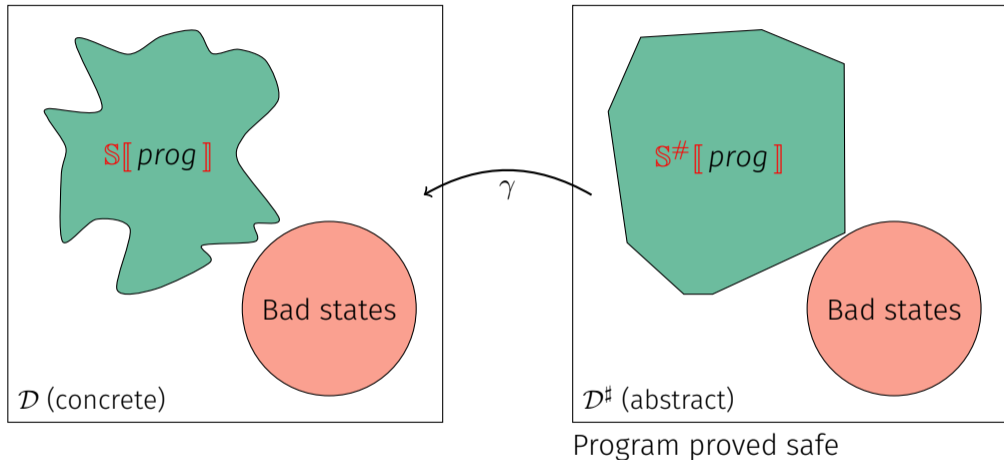


## Abstract interpretation – the big picture



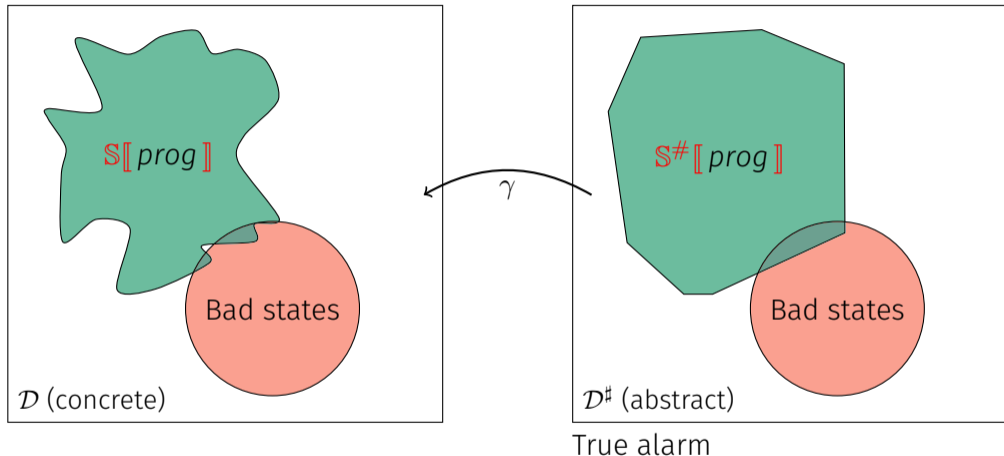
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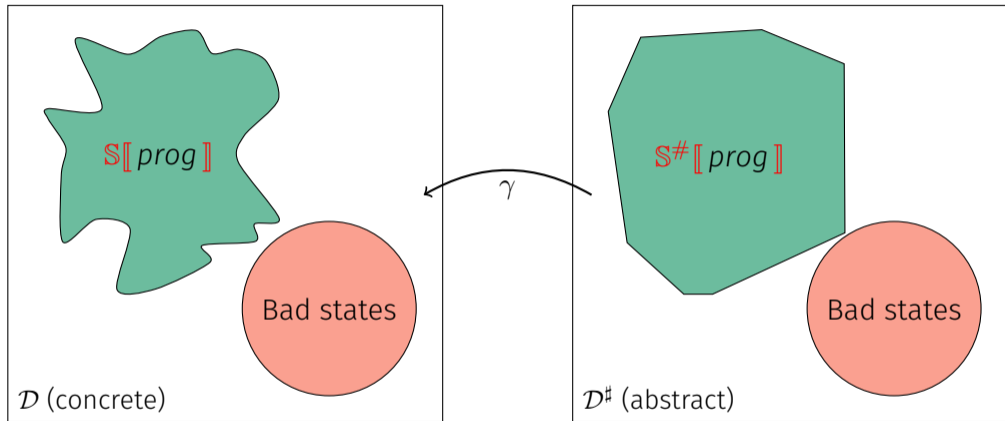
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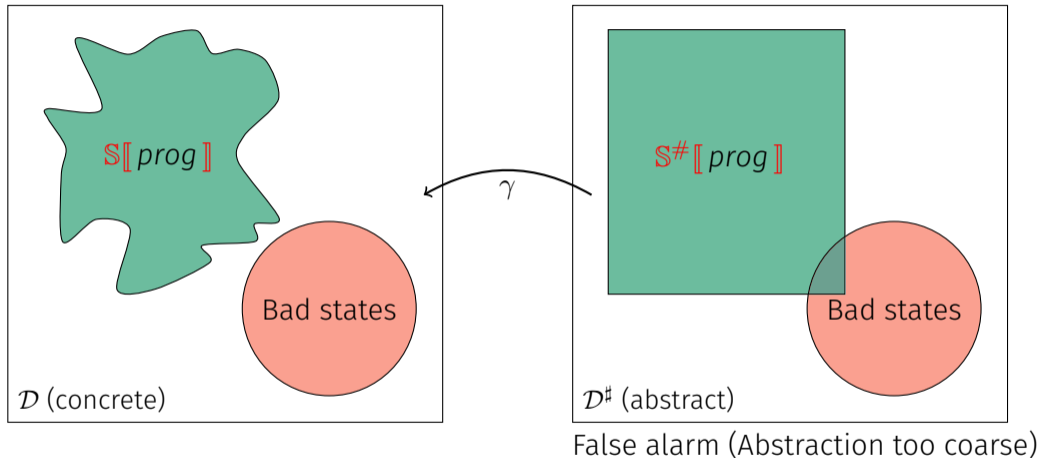


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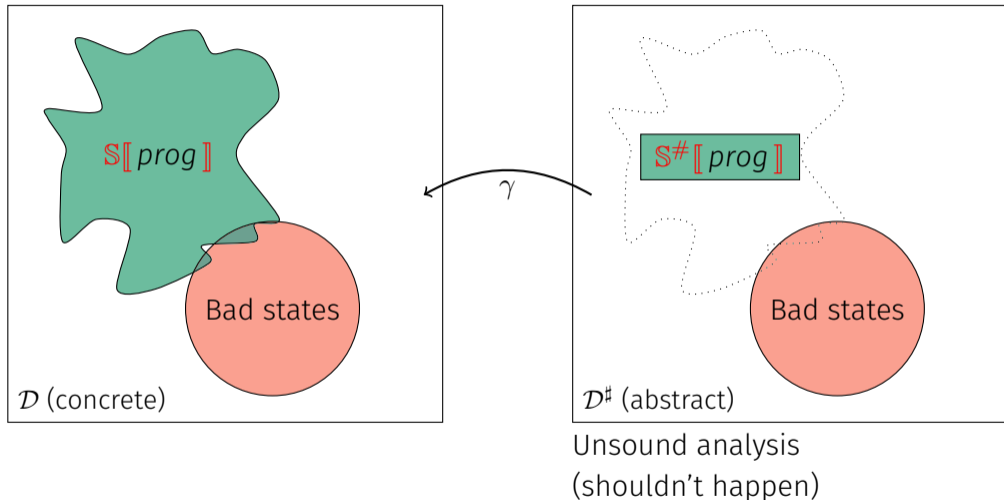
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# Critical software certification through static analysis



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# Critical software certification through static analysis



## Embedded C

- ▶ Generated code
- ▶ Dynamic allocation

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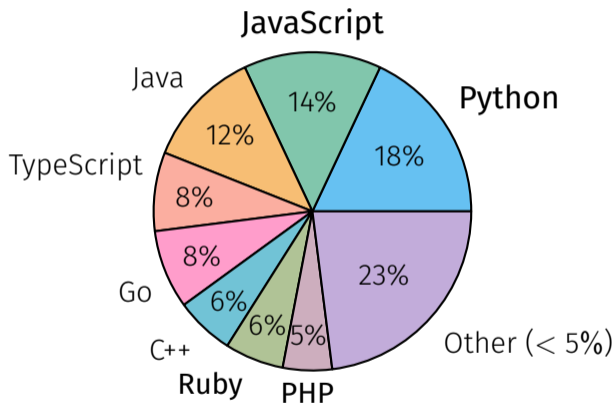
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## Democratizing static analysis?

- ▶ General C software (dynamic allocation, ...)
- ▶ Other languages
- ▶ Framework to implement analyses

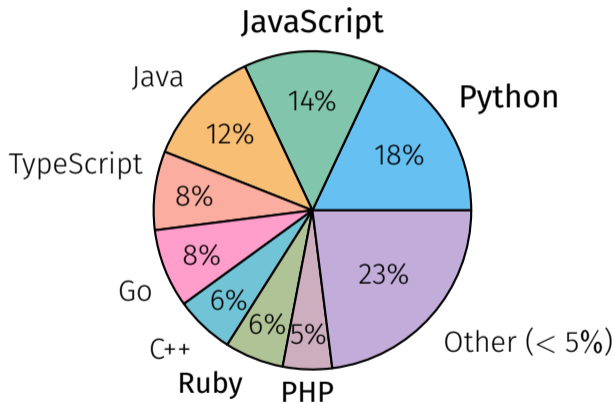
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## Dynamic programming languages



Most popular languages on GitHub

# Dynamic programming languages



Most popular languages on GitHub

## New features

- ▶ Dynamic typing
- ▶ Dynamic object structure



# Outline

- 1 Introduction
- 2 A Taste of Python
- 3 Analyzing Python Programs
- 4 Analyzing Python Programs with C Libraries
- 5 A Modern Compiler for the French Tax Code
- 6 Conclusion

# A Taste of Python

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## No standard

- ▶ CPython is the reference

⇒ manual inspection of the source code and handcrafted tests

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## Operator redefinition

- ▶ Calls, additions, attribute accesses
- ▶ Operators eventually call overloaded `__methods__`

### Protected attributes

```
1 class Protected:
2     def __init__(self, priv):
3         self._priv = priv
4     def __getattr__(self, attr):
5         if attr[0] == "_": raise AttributeError("...")
6         return object.__getattr__(self, attr)
7
8 a = Protected(42)
9 a._priv # AttributeError raised
```

## Python's specificities (II)

### Dual type system

- ▶ Nominal (classes, MRO)

Fspath (from standard library)

```
1 class Path:
2     def __fspath__(self): return 42
3
4 def fspath(p):
5     if isinstance(p, (str, bytes)):
6         return p
7     elif hasattr(p, "__fspath__"):
8         r = p.__fspath__()
9         if isinstance(r, (str, bytes)):
10            return r
11        raise TypeError
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13 fspath("/dev" if random() else Path())
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### Exceptions

Exceptions rather than specific values

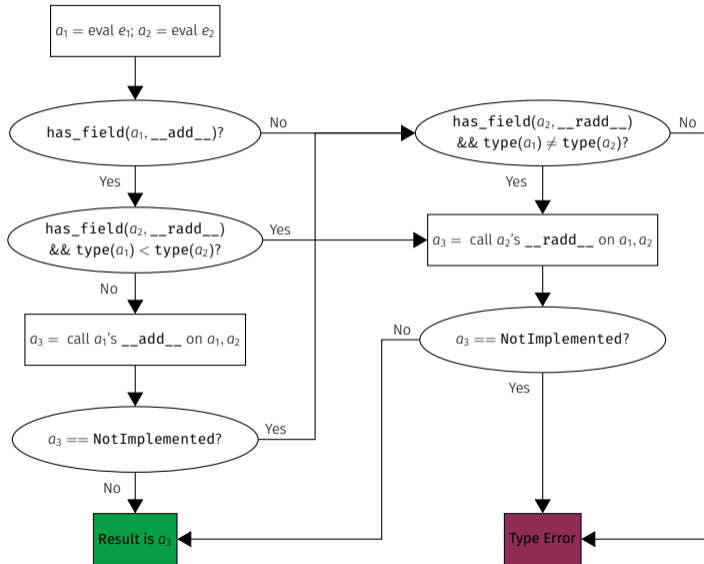
- ▶ `1 + "a" ↪ TypeError`
- ▶ `l[len(l) + 1] ↪ IndexError`

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## Example Semantics – binary operators





## Custom infix operators

```
1 class Infix(object):
2     def __init__(self, func): self.func = func
3     def __or__(self, other): return self.func(other)
4     def __ror__(self, other): return Infix(lambda x: self.func(other, x))
5
6 instanceof = Infix(isinstance)
7 b = 5 |instanceof| int
8
9 @Infix
10 def padd(x, y):
11     print(f"{x} + {y} = {x + y}")
12     return x + y
13 c = 2 |padd| 3
```

Credits [tomerriliba.com/blog/Infix-Operators/](https://tomerriliba.com/blog/Infix-Operators/)

# Analyzing Python Programs

---

### Goal

Detect runtime errors: uncaught raised exceptions

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## Supported constructs

Our analysis supports:

- ▶ Objects
- ▶ Exceptions
- ▶ Dynamic typing
- ▶ Introspection
- ▶ Permissive semantics
- ▶ Dynamic attributes
- ▶ Generators
- ▶ **super**
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## Unsupported constructs

- ▶ Recursive functions
- ▶ **eval**
- ▶ Finalizers

### Averaging numbers

```
1 def average(l):
2     m = 0
3     for i in range(len(l)):
4         m = m + l[i]
5     m = m // (i + 1)
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8 l = [randint(0, 20)
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Searching for a loop invariant (l. 4)

## Environment abstraction

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Stateless domains: **list content**,

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$$m \in [0, +\infty) \quad \underline{\text{els}}(l) \in [0, 20]$$
$$i \in [0, +\infty)$$

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## Numeric abstraction (polyhedra)

$$m \in [0, +\infty) \quad \underline{\text{els}}(l) \in [0, 20]$$
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## Averaging tasks

```
1 class Task:
2     def __init__(self, weight):
3         if weight < 0: raise ValueError
4         self.weight = weight
5
6     def average(l):
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## Attributes abstraction

$$@_{\text{Task}}^{\#} \mapsto (\{\text{weight}\}, \emptyset)$$

# Analysis | Domains required

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```

### Conclusion

- ▶ Different domains depending on the precision
- ▶ Use of auxiliary variables (underlined)

Searching for a loop invariant (l. 4)

Stateless domains: list content, list length

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$m \mapsto @^{\#} \dots i \dots @^{\#} \dots @^{\#} \text{Task}$

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# Modular Open Platform for Static Analysis<sup>1</sup>

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## Modular Open Platform for Static Analysis<sup>1</sup>




- ▶ One AST to analyze them all
  - 🚩 Multilanguage support
  - 📄 Expressiveness
  - ♻️ Reusability

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  - ▶  Semantic rewriting
  - ▶  Loose coupling
  - ▶  Observability

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- ▶ DAG of abstract domains
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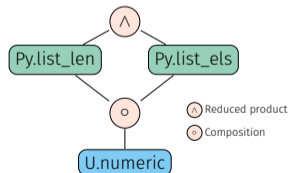


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Universal.Iterators.Loops

Matches `while(...){...}`

Computes fixpoint using widening

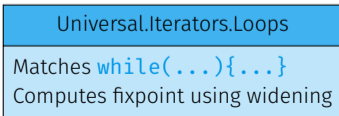
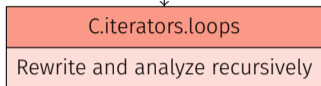
```
for(init; cond; incr) body
```

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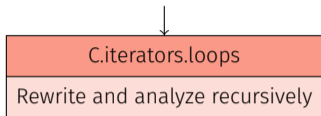
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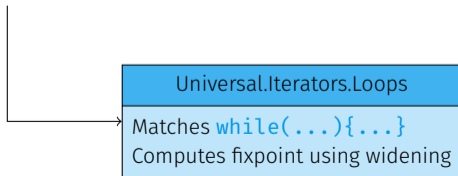
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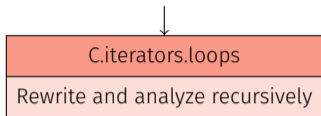


```
init;  
while(cond) {  
  body;  
  incr;  
}
```

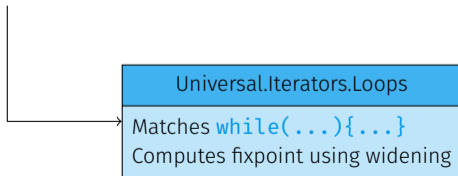


```
for(init; cond; incr) body
```

```
for target in iterable: body
```

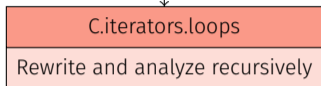


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init;  
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}
```

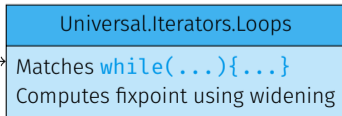


# Mopsa | Dynamic, semantic iterators with delegation

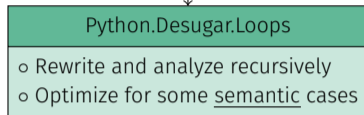
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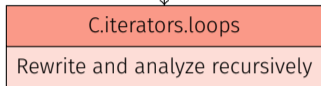
```
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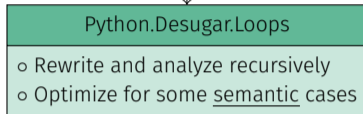
# Mopsa | Dynamic, semantic iterators with delegation

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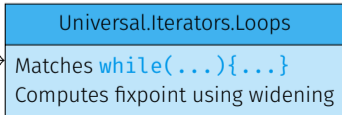


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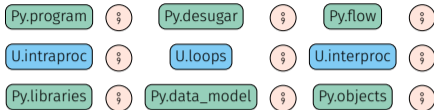
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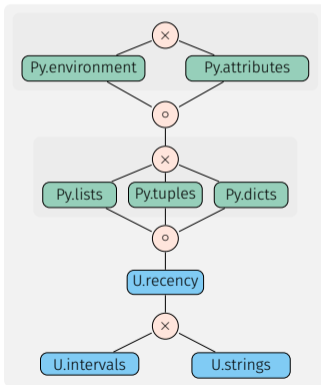
```
it = iter(iterable)  
while(1) {  
  try: target = next(it)  
  except StopIteration: break  
  body  
}  
clean it
```



# Definition of the Value Analysis



- Universal
- Python specific



- Sequence
- Cartesian product
- Composition

# Comparison of the type and value analyses

## Averaging tasks

```
1 class Task:
2     def __init__(self, weight):
3         if weight < 0: raise ValueError
4         self.weight = weight
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6     def average(l):
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13 l = []
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► ValueError (l. 3)

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## Non-relational value analysis










IndexError (l. 9)

## Relational value analysis










No alarm!



## Comparison of the type and value analyses (II)

Name	LOC	Type Analysis					Non-relational Value Analysis				
		Time	Mem.	Exceptions detected			Time	Mem.	Exceptions detected		
				Type	Index	Key			Type	Index	Key
 nbody.py	157	1.5s	3MB	0	22	1	5.7s	9MB	0	<b>1</b>	1
 scimark.py	416	1.4s	12MB	1	1	0	3.4s	27MB	1	<b>0</b>	0
 richards.py	426	13s	112MB	1	4	0	17s	149MB	1	<b>2</b>	0
 unpack_seq.py	458	8.3s	7MB	0	0	0	9.4s	6MB	0	0	0
 go.py	461	27s	345MB	33	20	0	2.0m	1.4GB	33	20	0
 hexiom.py	674	1.1m	525MB	0	46	3	4.7m	3.2GB	0	<b>21</b>	3
 regex_v8.py	1792	23s	18MB	0	2053	0	1.3m	56MB	0	<b>145</b>	0
 processInput.py	1417	10s	64MB	7	7	1	12s	85MB	7	<b>4</b>	1
 choose.py	2562	1.1m	1.6GB	12	22	7	2.9m	3.7GB	12	<b>13</b>	7
Total	9294	4.0m	2.8GB	59	2214	12	13m	9.1GB	59	228	12










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- The non-relational value analysis
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### Heuristic packing and relational analyses

- ▶ Static packing, using function's scope
- ▶ Rules out all 145 alarms of  regex\_v8.py (1792 LOC) at 2.5 $\times$  cost

# Analyzing Python Programs with C Libraries

---

One in five of the top 200 Python libraries contains C code

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- ▶ Garbage collection

# Combining C and Python – example

counter.c

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### Type annotations

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# How to analyze multilanguage programs?

Type annotations

Rewrite into Python code

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- ▶ Some effects can't be written in pure Python (e.g., read-only attributes)

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Drawbacks of the current approaches



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Our approach

- ▶ Analyze both the C and Python sources
- ▶ Switch from one language to the other just as the program does
- ▶ Reuse previous analyses of C and Python
- ▶ Detect runtime errors in Python, in C, and at the boundary



# Analysis result

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### Difficulty: shared memory

- ▶ Each language may change the memory state, and has a different view of it
- ▶ Synchronization? We could perform a full state translation, but
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  - some abstractions can be shared between Python and C

# High-level idea

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## State separation $\rightsquigarrow$ reduced synchronization

- ▶ Observation: structures are directly dereferenceable by one language only
- ▶ Switch to other language otherwise (`c.incr()`  $\rightsquigarrow$  `self->count += 1`)  
Additional hypothesis: C accesses to Python objects through the API
- ▶ Synchronization: only when objects change language for the first time
- ▶ Mopsa supports shared abstractions

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- ▶ Garbage collection not handled
- ▶ C access to Python objects only through the API (verified by Mopsa)

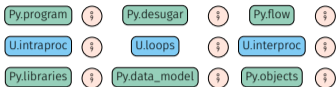
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- ▶ Defines the API: calls between languages, value conversions
- ▶ Boundary functions handling the reduced synchronization

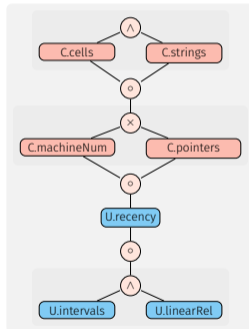
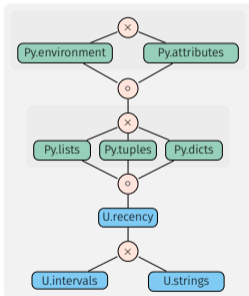
## Limitations

- ▶ Garbage collection not handled
- ▶ C access to Python objects only through the API (verified by Mopsa)
- ▶ Manual modelization from CPython's source code

# From distinct Python and C analyses...

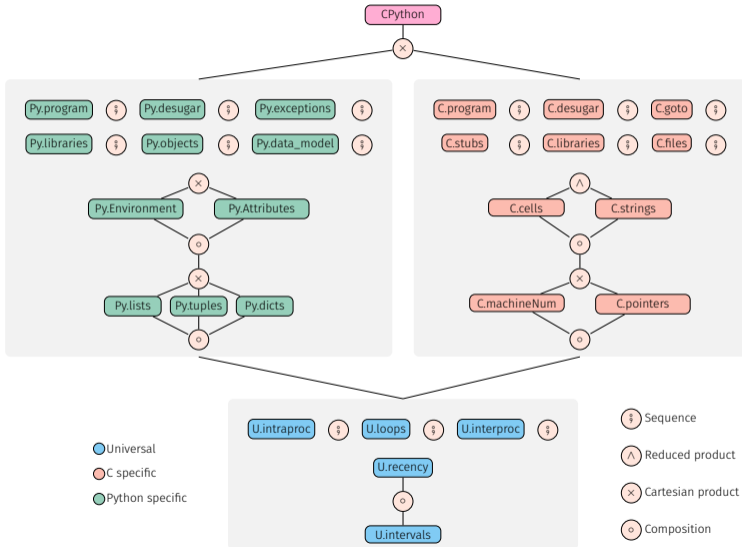


- Universal
- C specific
- Python specific

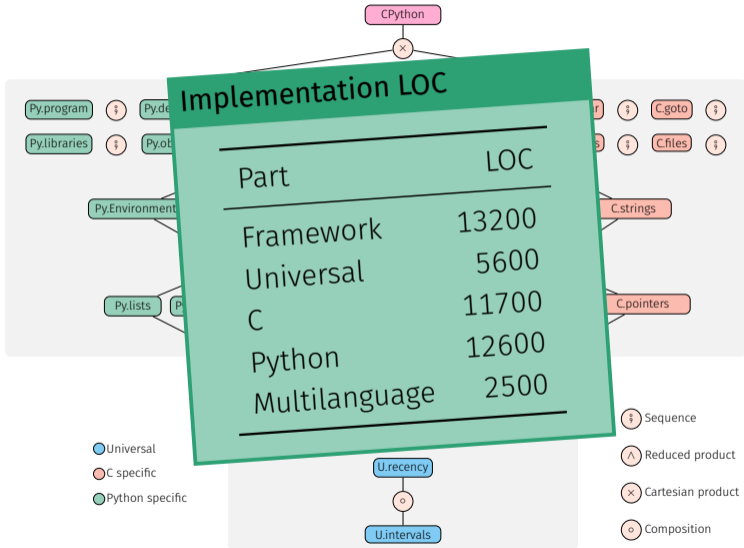


- Sequence
- ∧ Reduced product
- × Cartesian product
- Composition

# From distinct Python and C analyses... to a multilanguage analysis!



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## Corpus selection

- ▶ Popular, real-world libraries available on GitHub, averaging 412 stars.
- ▶ Whole-program analysis: we use the tests provided by the libraries.

Library	C + Py. Loc	Tests	🕒/test	$\frac{\# \text{ proved checks}}{\# \text{ checks}} \%$	# checks
noise	1397	15/15	1.2s	99.7%	(6690)
cdistance	2345	28/28	4.1s	98.0%	(13716)
l1ist	4515	167/194	1.5s	98.8%	(36255)
ahocorasick	4877	46/92	1.2s	96.7%	(6722)
levenshtein	5798	17/17	5.3s	84.6%	(4825)
bitarray	5841	159/216	1.6s	94.9%	(25566)

## Python's semantics



- ▶ Reverse-engineering CPython (160kLoc C)
- ▶ Backlinks to source code (auditability)
- ▶ On-paper formalization ( $\simeq$  44 pages)



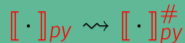
# Contributions around the static analysis of Python programs

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- ▶ Type and value analyses
- ▶ Combining numerous abstractions
- ▶ Analysis of real programs

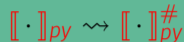
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## Implementation into Mopsa

- ▶ Open-source analyzer for C and Python
- ▶ Factors abstractions between languages
- ▶ Sharing between abstractions

# A Modern Compiler for the French Tax Code

---

**Research field: formal methods**

⇒ Improve confidence in software.

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⇒ Improve confidence in software.

### Personal methodology


Constant back and forth between theory and practice

- 1 Find interesting bugs, properties or systems to study (GitHub, ...)
- 2 Theoretical study and solution
- 3 Implementation and experimental validation (on 1)

## French income tax

- ▶ 38M households, 75Md€ of income
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## Trusting the computation?

- ▶ Reproducibility of the computation?
- ▶ Accurate simulation of tax reforms?
- ▶ Compliance with the law, acting as specification?



### Variable declaration

```
IRNETBIS : calculee primrest = 0 : "IRNET avant bidouille du 8ZI" ;  
8ZI : "Impot net apres depart a l'etranger (non residents)" ;
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### Computation rule

```
rule 221220:  
application : iliad ;  
IRNETBIS = max(0, IRNETTER -  
                PIR * positif(SEUIL_12 - IRNETTER + PIR)  
                * positif(SEUIL_12 - PIR)  
                * positif_ou_nul(IRNETTER - SEUIL_12));
```

The core of M: **arithmetic expressions** assigned to variables.

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### M quirks

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- ▶ Static-size arrays (size defined at declaration)
- ▶ Small, unrollable loops
- ▶ Use of floating-point numbers, booleans are zero and one
- ▶ `undef` value

We reverse-engineered the semantics:

- ▶ At first, using the online simulator<sup>2</sup>
- ▶ Later, using the private tests DGFIP sent us (August 7, 2019)

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⇒ a  $\mu$ M kernel, its semantics formalized in the Coq proof assistant.

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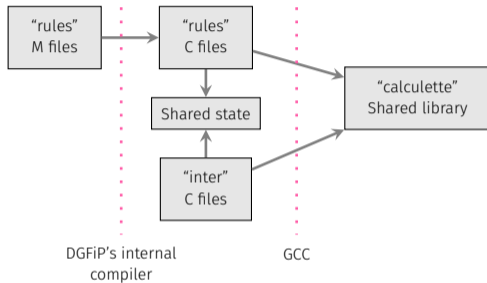
### The **undef** value

- ▶ Used for: default inputs, runtime errors & missing cases in inline conditionals
- ▶ Fun facts:  $f + \mathbf{undef} = f$ ,  $f \div 0 = 0$ ,  $x[|x| + 1] = \mathbf{undef}$ ,  $x[-1] = 0$ ...

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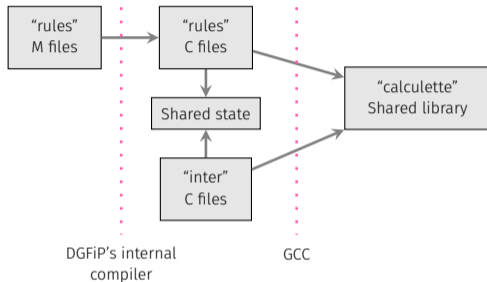
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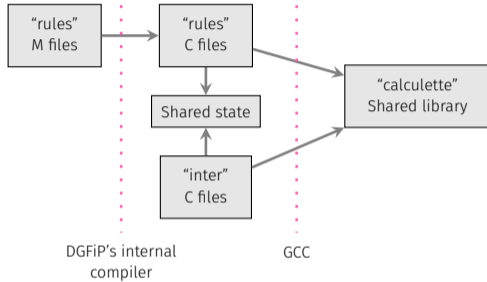


## "inter" files

35kLoc of C to bypass M's lack of functions.

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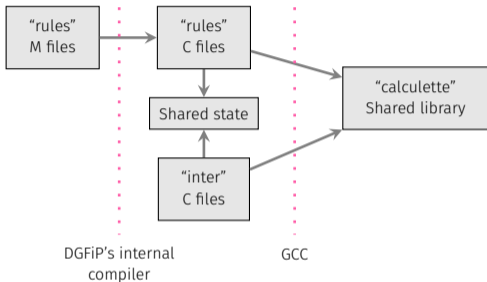
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**Security concerns**  $\rightsquigarrow$  no publication

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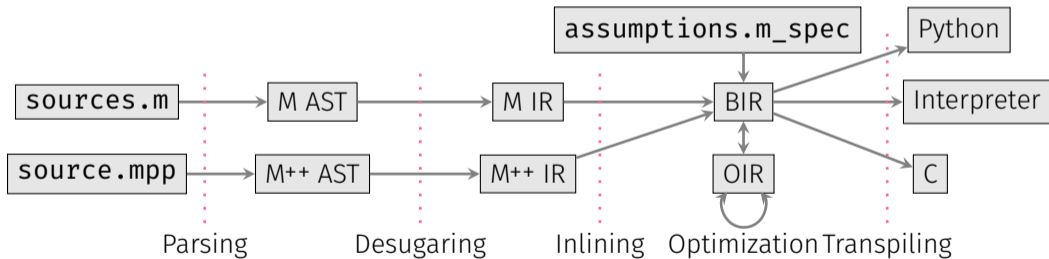
## DSLs to the rescue! Introducing M++

- ▶ High-level, no mutable state under the hood
- ▶ Tailored for the needs of the "inter" files and DGFIP devs
- ▶ 6,000 lines of "inter" C code  $\Rightarrow$  100 lines of M++

MLANG: written in OCaml, 10k lines of code  
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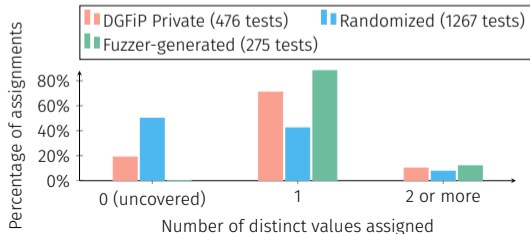
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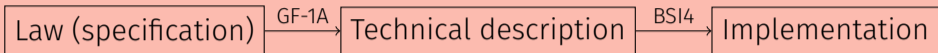
Ongoing work to bring MLANG at DGFIP.

- ▶ 30-day mission between January and August 2022
- ▶ Supervision of 3 developers (2 OCamlPro, 1 DGFIP)

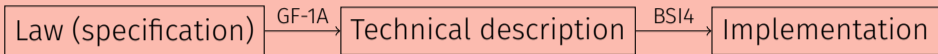
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Does the implementation comply with the law?



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- ▶ No structural correspondance
- ▶ 2019↔2020 : 30% of 90kLoc M changed

## Does the implementation comply with the law?

### Catala, another DSL to the rescue

#### Article D521-1 du code de la sécurité sociale

I - Pour l'application de l'article L. 521-1, le montant des allocations familiales et de la majoration pour âge prévue à l'article L. 521-3 est défini selon le barème suivant :

1° Lorsque le ménage ou la personne a disposé d'un montant de ressources inférieur ou égal au plafond défini au I de l'article D. 521-3, les taux servant au calcul des allocations familiales sont fixés, en pourcentage de la base mensuelle prévue à l'article L. 551-1, à :

a) 32 % pour le deuxième enfant à charge ;

```
```catala
champ d'application AllocationsFamiliales :
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    ressources_ménage ≤€ plafond_I_d521_3
  conséquence égal à
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    sinon 0 €
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- ▶ Literal programming
- ▶ Default logic
- ▶ Participation to dev. team & interdisciplinary meetings
- ▶ Future: automated verification for Catala?

## Conclusion

---

## Summary of the contributions

### Static analysis of Python programs using C libraries

- ▶ Ouadjaout and Miné (LIP6, Sorbonne Université)
- ▶ SAS'21<sup>🏆</sup>, ECOOP'20<sup>🏆</sup>, VSTTE'19 (invited), SOAP@PLDI'20 (award), JFLA'21 (fr, tool)
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### A modern compiler for the French tax code

- ▶ Merigoux (Prosecco, Inria Paris) et Protzenko (Microsoft Research)
- ▶ CC'21<sup>🏆</sup>, JFLA'20 (fr), JFLA'21 (fr, tool)
- ▶ Mlang (GPL v3, 10kLoc OCaml), main contributor since May 2019
- ▶ Ongoing transfer work
  - 30 days mission between January and August 2022
  - Supervision of 3 developers (2 OCamlPro, 1 DGFIP)

Looking forward... an important question

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- ⚠️ Avoiding rebound effect
- ❓ Impact? Difficult to estimate a priori

# From Python to the French Tax Code: Applying Formal Methods on Real Systems

## Discussion

Interested in internships or PhDs?

Raphaël Monat

SyCoMoRES team

rmonat.fr

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Interested in internships or PhDs?  
Come have a chat or email me!  
[raphael.monat@inria.fr](mailto:raphael.monat@inria.fr)

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